



# Quantitative evaluation of the effects of bycatch on native species using mathematical models

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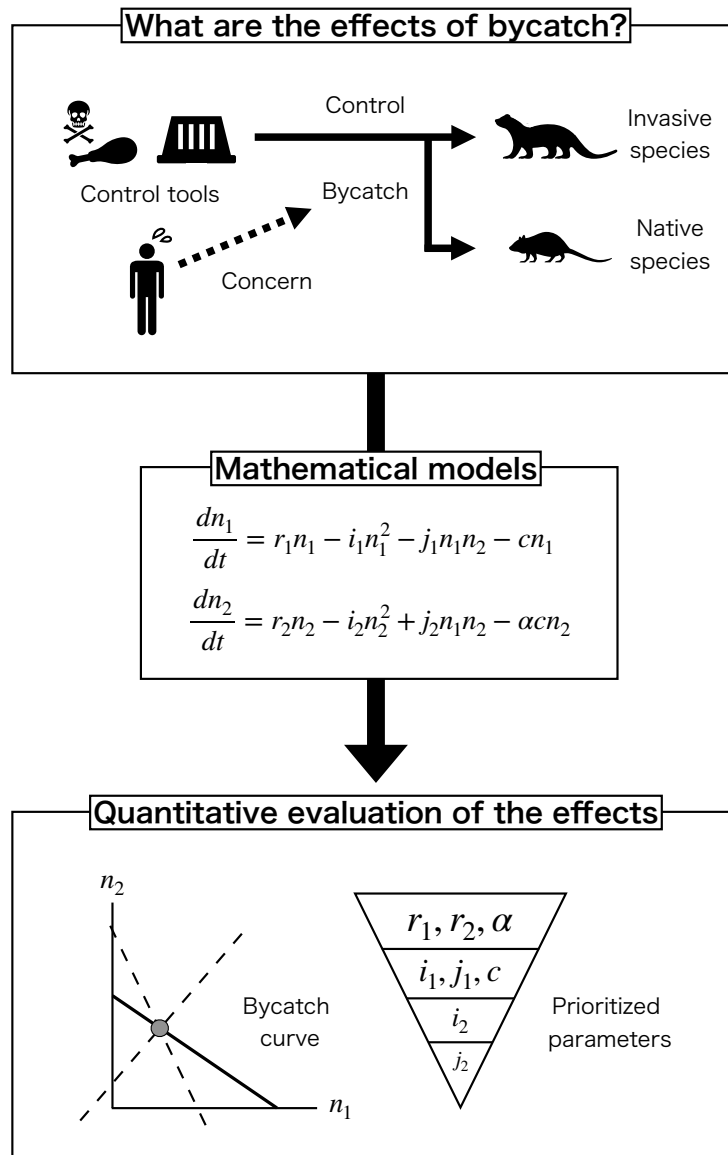
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# Graphical Abstract

## Quantitative evaluation of the effects of bycatch on native species using mathematical models

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## Highlights

### **Quantitative evaluation of the effects of bycatch on native species using mathematical models**

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- Bycatch curve was defined to show the density changes of native and invasive species
- Parameter priority was determined for estimation in actual control programs
- With intrinsic growth rates and specific killing rate, control success is determined
- With some parameters, the simple model gives approximate density changes of species
- With sufficient parameters, the basic model gives eradication goals in detail

# Quantitative evaluation of the effects of bycatch on native species using mathematical models

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## Abstract

Traps and poison bait are used to control invasive species and protect native species. However, the traps can kill native species and the poison bait may increase their mortality. As it interferes with conservation efforts, it is necessary to evaluate the effects of such bycatch. However, there are few theoretical methods for quantification of these effects.

This paper presents a method for quantitatively evaluating the effects of bycatch on native populations, using a mathematical model that represents the population dynamics of native and invasive species.

The mathematical model suggested the conditions under which only invasive species will be eliminated even if bycatch occurs. We also present the concept of the "bycatch curve", which shows the population density according to the killing rate. In addition, a mathematical simulation is presented using parameters estimated for the Amami-Oshima system.

These theoretical results allowed us to determine the parameters that should be prioritized for estimation in actual control programs.

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*Keywords:* Bycatch, Conservation, Control programs, Invasive species,  
Native species, Parameter priority

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## 1. Introduction

Invasive species have a serious impact on native populations and can threaten their survival (Courchamp, Chapuis, et al., 2003). Mongooses and rats appear in “100 of the World’s Worst Invasive Alien Species ” (Lowe et al., 2000), and their introduction into a closed system such as an island, where population immigration and emigration can be neglected, subjects native species to greater predation and competition over a shorter period of time than in an open system, such as the mainland (Hays & Conant, 2007; Shiels et al., 2014). Control programs in closed systems must be based on prompt and accurate surveys (Courchamp, Chapuis, et al., 2003).

There are two main types of control methods: traditional and biological methods (Courchamp, Chapuis, et al., 2003). Traditional methods include fencing, shooting, poisoning, and trapping. Traps are mainly used for mongooses (Hays & Conant, 2007), while traps and poison bait are employed for rats (Shiels et al., 2014). However, these methods may increase the mortality rate of native species. This unintended increase in mortality is called bycatch, and has already been recognized in marine systems (Hall et al., 2000; Lewison et al., 2004; Davies et al., 2009). However, it is also becoming increasingly problematic in terrestrial systems. For example, on Amami-Oshima Island, Japan, traps have been used to control the small Indian mongoose [*Herpestes*

21 *auropunctatus*] (Watari, Takatsuki, et al., 2008; Fukasawa, Hashimoto, et  
22 al., 2013; Watari, Nishijima, et al., 2013), but as the mongoose population  
23 declined, the mortality of native species, such as the Amami spiny rat [*Toku-*  
24 *daia osimensis*] and the Ryukyu long-haired rat [*Diplothrix legata*], increased  
25 due to bycatch (Fukasawa, Miyashita, et al., 2013), which made it difficult  
26 to continue the control program (Watari 2011). In New Zealand, rats and  
27 possums have been eradicated by poison bait, such as brodifacoum and com-  
28 pound 1080 [*sodium monofluoroacetate*] (Innes & Barker, 1999; Howald et  
29 al., 2007). These methods have increased the mortality of native species,  
30 and also caused secondary poisoning of predators of invasive species (Rmp-  
31 son & Miskelly, 1999; Powlesland et al., 1999; Eason et al., 2002), rising  
32 concerns about their use (Veitch & Clout, 2001; Courchamp, Chapuis, et al.,  
33 2003; Towns et al., 2006; Howald et al., 2007).

34 To prevent the unintended death of native species, it is necessary to eval-  
35 uate bycatch by conducting detailed surveys, examining control plans, and  
36 predicting outcomes (Cromarty et al., 2002; Courchamp, Chapuis, et al.,  
37 2003). Bycatch has been quantified by field monitoring (Taylor & Thomas,  
38 1993; Dowding et al., 1999; Empson & Miskelly, 1999; Powlesland et al.,  
39 1999; Eason et al., 2002) and statistical estimation (Armstrong et al., 2002;  
40 Watari, Nishijima, et al., 2013; Alderman et al., 2019), but there are few op-  
41 tions available for theoretical evaluation. Some studies have proposed that  
42 it is necessary to kill all invasive species to prevent a negative impact on  
43 native species (e.g., Cromarty et al., 2002), whereas others have argued that

44 invasive species should merely be minimized in consideration of bycatch (e.g.,  
45 Eason et al., 2002; Courchamp et al., 2003; Howald et al., 2007). However,  
46 there is no method for determining the most appropriate control strategy.

47 We constructed differential equation models to resolve these problems.  
48 Our models are similar to previous differential equation models of consider  
49 bycatch (Pascoe, 1997; Anderson & Seijo, 2010; Clark, 2010). However,  
50 previous bycatch models were constructed for resource management and eco-  
51 nomic applications in the context of marine systems; by contrast, our model  
52 was designed for conservation applications in terrestrial systems, and pro-  
53 vides a means to quantify the consequences of bycatch and determine the  
54 most appropriate control strategy.

## 55 **2. Methods**

56 We constructed mathematical models to describe the dynamics of native  
57 and invasive populations. As predation by invasive species, such as mon-  
58 gooses and rats, is a major factor in the decline of native species (Courchamp,  
59 Chapuis, et al., 2003; Hays & Conant, 2007; Shiels et al., 2014), this study  
60 assumed that the density of native species is negatively correlated with that  
61 of invasive species. In addition, this study focused on a closed system. Based  
62 on these assumptions, a simple Lotka-Volterra model with logistic growth was  
63 used to model changes in the population density of two species in the absence

64 of control (Volterra 1926; Pearl & Reed, 1977; Berryman 1992; Lotka 2002),

$$\begin{aligned}\frac{dn_1}{dt} &= r_1n_1 - i_1n_1^2 - j_1n_1n_2, \\ \frac{dn_2}{dt} &= r_2n_2 - i_2n_2^2 + j_2n_1n_2.\end{aligned}\tag{1}$$

65 The upper and lower equations represent the native and invasive popula-  
66 tions, respectively, where  $n_1, n_2$  are the population densities,  $r_1, r_2$  are the  
67 intrinsic growth rates,  $i_1, i_2$  are the intraspecific interaction coefficients, and  
68  $j_1, j_2$  are the interspecific interaction coefficients. All parameters are positive  
69 and carrying capacities can be expressed as  $k_1 = r_1/i_1$ ,  $k_2 = r_2/i_2$ . The  
70 functional response was assumed to be mass-action because invasive species,  
71 such as mongooses and rats, are often omnivorous and their interactions are  
72 approximately random (Hays & Conant, 2007; Shiels et al., 2014).

73 A term representing bycatch is used in our model:

$$\begin{aligned}\frac{dn_1}{dt} &= r_1n_1 - i_1n_1^2 - j_1n_1n_2 - cn_1, \\ \frac{dn_2}{dt} &= r_2n_2 - i_2n_2^2 + j_2n_1n_2 - \alpha cn_2,\end{aligned}\tag{2}$$

74 where  $c$  is the killing rate of native species, and  $\alpha$  is the “specific killing  
75 rate” of invasive species, which generally satisfies  $1 \leq \alpha$ .  $\alpha$  and  $c$  satisfy  
76  $0 \leq \alpha c \leq 1$ , as it is obviously not possible to kill more individuals of an  
77 invasive species than exist. These linear terms reflect the fact that traps and  
78 poison bait are often arranged uniformly in spatial terms (Powlesland et al.,  
79 1999; Alderman et al., 2019).

### 80 3. Results

Model (2) behaves in three distinct ways depending on the population parameters. Based on the results of Gause & Witt (1935), we reformulated the model (2) using  $r'_1 = r_1 - c$ ,  $r'_2 = r_2 - \alpha c$ :

$$\frac{dn_1}{dt} = r'_1 n_1 - i_1 n_1^2 - j_1 n_1 n_2, \quad (3)$$

$$\frac{dn_2}{dt} = r'_2 n_2 - i_2 n_2^2 + j_2 n_1 n_2. \quad (4)$$

81 These equations describe three behaviors:

$$\left\{ \begin{array}{ll} \text{(a) Native species become extinct and only invasive species survive,} \\ \text{if } i_2/j_1 \leq r'_2/r'_1 \\ \text{(b) Both native and invasive species survive,} \\ \text{if } -j_2/i_1 < r'_2/r'_1 < i_2/j_1 \\ \text{(c) Invasive species become extinct and only native species survive,} \\ \text{if } r'_2/r'_1 \leq -j_2/i_1 \end{array} \right. \quad (5)$$

82 If the system is in state (a) and the native population is threatened with  
 83 extinction, the condition  $i_2/j_1 \leq r'_2/r'_1$  is considered to be satisfied because  
 84 the predation pressure on native species  $j_1$  is sufficiently greater than the  
 85 density dependence of invasive species  $i_2$ . In this case, extinction of native  
 86 species must be avoided by increasing the killing rate  $c$ ; this paper considers

87 the case where the killing rate  $c$  is increased from state (a).

88 Increasing  $c$  yields two different results depending on whether the specific  
 89 killing rate  $\alpha$  satisfies the following inequality:

$$\alpha > r_2/r_1. \quad (6)$$

90 When (6) holds,  $r'_2/r'_1$  decreases monotonically with respect to  $c$ , and the  
 91 dynamical system reaches (b) at  $c = c_\beta$  and (c) at  $c = c_\gamma$ .  $c_\beta$  and  $c_\gamma$  are  
 92 expressed as:

$$c_\beta = \frac{r_2 j_1 - r_1 i_2}{\alpha j_1 - i_2}, \quad c_\gamma = \frac{r_2 i_1 + r_1 j_2}{\alpha i_1 + j_2}. \quad (7)$$

93 As these values are given explicitly, they can be used as target values for the  
 94 control program. On the other hand, when the population parameters do not  
 95 satisfy (6),  $r'_2/r'_1$  increases monotonically or remains unchanged with respect  
 96 to  $c$ , and the system maintains state (a). Thus, to prevent the extinction of  
 97 native species, we have to ensure that  $\alpha > r_2/r_1$  is valid.

98 When the system is in state (b) and equilibrium, we are able to visualize  
 99 the density changes of two species caused by the control program. Nullclines  
 100 in (2) (when the system is in equilibrium) satisfy:

$$\begin{aligned} r_1 - i_1 n_1 - j_1 n_2 - c &= 0, \\ r_2 - i_2 n_2 + j_2 n_1 - \alpha c &= 0. \end{aligned} \quad (8)$$

101 Eliminating  $c$  from these equations, a single curve is obtained:

$$n_1 = \frac{(\alpha r_1 - r_2) - (\alpha j_1 - i_2)n_2}{(\alpha i_1 + j_2)}. \quad (9)$$

102 When  $c$  is varied, the fixed point of coexistence moves along the curve. Thus,  
 103 this curve represents the change in density of invasive and native species when  
 104 the killing rate  $c$  is modified in the control plan. We defined this curve as  
 105 the “bycatch curve” (Fig. 1). If  $\alpha > r_2/r_1$  and  $j_1 > i_2$  hold, the bycatch  
 106 curve passes through the first quadrant and satisfies  $c = c_\beta$  at the fixed point  
 107 that intersects with the  $n_2$  axis, and satisfies  $c = c_\gamma$  at the fixed point  
 108 intersects with the  $n_1$  axis. The bycatch curve can be adapted even though  
 109 the interaction term is more complex, but the fixed point of coexistence must  
 110 be stable.

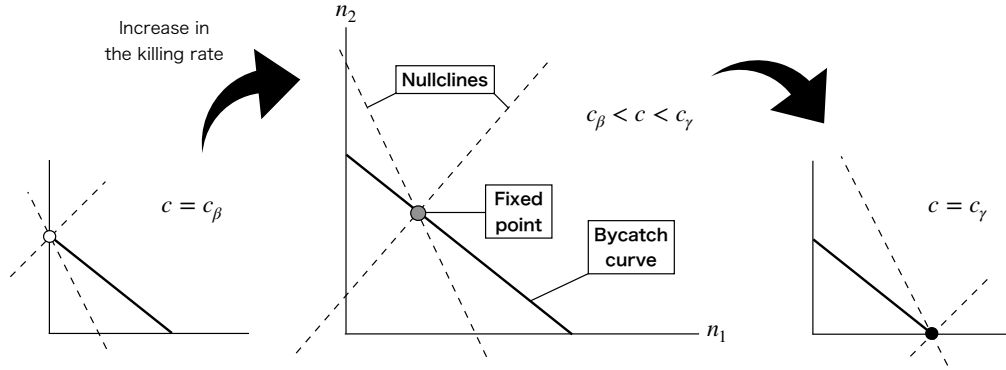


Figure 1: Concept of the bycatch curve (9). When (6) is satisfied, it represents the trajectory of a fixed point with variation of the killing rate  $c$  on the phase plane, and  $c_\beta, c_\gamma$  are the targets of the control.

111 Using this model, we performed an example simulation assuming that

112 the Amami spiny rat is a native species and the small Indian mongoose is an  
 113 invasive species. From Bayesian estimations conducted in previous studies  
 114 (Fukasawa, Hashimoto, et al., 2013; Watari, Nishijima, et al., 2013), the  
 115 values of the population parameters were set to  $r_1 = 8$ ,  $i_1 = 0.4$ ,  $j_1 =$   
 116  $0.4$ ,  $r_2 = 0.5$ ,  $i_2 = 0$ ,  $n_1(0) = k_1 = 20$ . Assuming that the the control  
 117 gradually increases,  $c$  is set to increase linearly  $c = 0.01 \cdot t$  (where  $t$  is year).  
 118 As  $j_2$  and  $n_2(0)$  were not estimated in previous studies,  $j_2$  was set to 0.01  
 119 assuming a conversion rate of about  $1/40$ , and  $n_2(0)$  was set to 0.01 because  
 120 the number of initially introduced individuals was very small. In the absence  
 121 of control ( $c = 0$ ), the system is in state (a) because  $i_2/j_1 = 0$  and  $r_2/r_1 =$   
 122  $0.0625$  satisfy the condition  $i_2/j_1 < r_2/r_1$ . If the specific killing rate  $\alpha$  exceeds  
 123 the threshold  $r_2/r_1 = 0.0625$ , the system can be transitioned to state (b) or  
 124 (c) by increasing the killing rate  $c$ . When  $\alpha = 1, 2, 3$ , the goals of the killing  
 125 rate  $c_\beta = 0.50/\alpha$ ,  $c_\gamma = 0.28/(0.4\alpha + 0.01) \sim 0.70/\alpha$  are, respectively:

$$\left\{ \begin{array}{l} \alpha = 1 : c_\beta = 0.50, c_\gamma \sim 0.70 \\ \alpha = 2 : c_\beta = 0.25, c_\gamma \sim 0.35 \\ \alpha = 3 : c_\beta = 0.17, c_\gamma \sim 0.23 \end{array} \right. \quad (10)$$

126 As the linearly increasing  $c$  becomes 0.20 in 20 years and 0.40 in 40 years,

127 the simulation results (Fig. 2: left) are interpreted as follows:

$$\left\{ \begin{array}{l} \alpha = 1 : \text{The control is very low,} \\ \qquad \qquad \text{and only the native species goes extinct.} \\ \alpha = 2 : \text{The control is not sufficient,} \\ \qquad \qquad \text{and the native species goes extinct before the invasive species.} \\ \alpha = 3 : \text{The control is sufficiently high,} \\ \qquad \qquad \text{and only the invasive species goes extinct.} \end{array} \right. \quad (11)$$

128 It seems that  $\alpha = 1, 2$  cannot protect native species, but  $\alpha = 3$  facilitates  
 129 their conservation. In the case of  $\alpha = 3$ , it may be assumed that the number  
 130 of invasive species has not decreased in the middle of the eradication period  
 131 (e.g., 20th year), and that eradication cannot be achieved; this is reasonable  
 132 when comparing the killing rate at that time (0.20) with the target ( $c_\gamma \sim$   
 133 0.23).

#### 134 4. Discussion

135 It has been suggested that the negative impact of bycatch on native  
 136 species is smaller than that of invasive species (Innes & Barker, 1999; Hays &  
 137 Conant, 2007; Jones et al., 2016), but there is no real theoretical basis for this  
 138 opinion. This paper suggested that only the invasive population will become  
 139 extinct by increasing the killing rate if  $\alpha > r_2/r_1$  and  $j_1 > i_2$  hold. When we

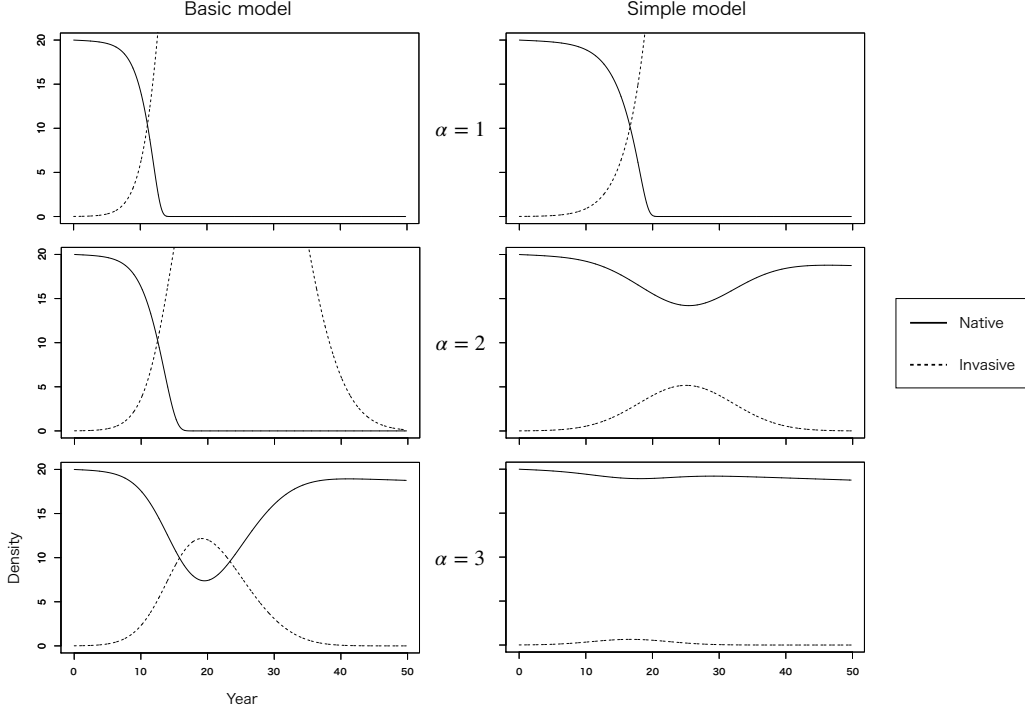


Figure 2: Example simulation using model (2) [Left] and model (12)[Right]. The value of the parameters and initial conditions were set to  $r_1 = 8$ ,  $i_1 = 0.4$ ,  $j_1 = 0.4$ ,  $r_2 = 0.5$ ,  $i_2 = 0$ ,  $j_2 = 0.01$ ,  $c = 0.01 \cdot t$ ,  $n_1(0) = 20$ ,  $n_2(0) = 0.01$ , where  $t$  is year.

140 can configure  $\alpha$  to satisfy  $\alpha > r_2/r_1$ , this opinion is theoretically supported.  
 141 When this condition is satisfied,  $c_\beta$  and  $c_\gamma$  are important values for the killing  
 142 rate. As  $c_\beta$  is the minimum killing rate at which native species survive and  $c_\gamma$   
 143 is the minimum killing rate at which invasive species go extinct, the former  
 144 can serve as the first goal of eradication, and the latter as the ultimate goal.  
 145 In addition, using the bycatch curve, we can visualize the path of a fixed  
 146 point on the phase plane as the killing rate changes. As this concept rep-  
 147 resents only the equilibrium state, it may not provide detailed information

148 on the behavior of the system in the non-equilibrium state. However, it can  
149 be a useful indicator when implementing long-term plans in which there is  
150 sufficient time for the system to reach equilibrium.

151 To apply these results in real projects, information on population pa-  
152 rameters is necessary. For example, there are classically static and dynamic  
153 approaches for estimating intraspecific  $i$  and interspecific interaction coef-  
154 ficients  $j$  (MacArthur & Levins, 1967; Seifert & Seifert, 1976; Shenbrot &  
155 Krasnov, 2002). When estimating these interactions for invasive species, it is  
156 necessary to use a dynamic approach that can be adapted to non-equilibrium  
157 conditions, rather than a static approach that assumes equilibrium conditions  
158 (Shenbrot & Krasnov, 2002). In statistical estimations, Bayesian estima-  
159 tion is considered to be useful because it can take into account uncertainty  
160 (Watari, Nishijima, et al., 2013; Alderman et al., 2019).

161 It may be ideal to estimate all parameters, but it is difficult to evaluate the  
162 interactions of invasive species when we do not have time to collect enough  
163 data or the density of native species is low at the outset of the project. In  
164 these cases, a simple approach would be useful. The model (2) assumes that  
165 invasive species have negative density dependence and benefit from predation  
166 on the native species, but if the invasive species is still increasing and the  
167 native species is already low-density, these effects are expected to be smaller

168 than those of other terms. The model (2) is then simplified as follows:

$$\begin{aligned}\frac{dn_1}{dt} &= r_1 n_1 - i_1 n_1^2 - j_1 n_1 n_2 - c n_1, \\ \frac{dn_2}{dt} &= r_2 n_2 - \alpha c n_2.\end{aligned}\tag{12}$$

169 This model has the solutions:

$$\begin{aligned}n_1(t) &= \frac{e^{A(t)}}{e^{A(0)}/n_1(0) - \int_0^t i_1 e^{A(\tau)} d\tau}, \\ n_2(t) &= n_2(0) e^{\int_0^t (r_2 - \alpha c) d\tau}, \\ A(\tau) &= \int (j_1 n_2(\tau) + c - r_1) d\tau.\end{aligned}\tag{13}$$

170 Here, the eradication goals of invasive species  $\alpha c_\beta$  and  $\alpha c_\gamma$  correspond to the  
171 intrinsic growth rate of invasive species  $r_2$ . Model (12) enables us to broadly  
172 understand the population dynamics with only six parameters,  $r_1$ ,  $r_2$ ,  $i_1$ ,  $j_1$ ,  
173  $c$ ,  $\alpha$ , but it should again be noted that this approach is justified only if  $i_2 \sim 0$   
174 and  $j_2 \sim 0$  hold.

175 Example simulations from (2) and (12) are shown in (Fig. 2). The actual  
176 killing rate imposed on invasive species in Amami is considered to be roughly  
177  $\alpha c = 0.02 \cdot t$  (Fukasawa, Hashimoto, et al., 2013). This result corresponds to  
178 the current Amami condition, where native species have disappeared around  
179 the area where the mongoose was introduced (Watari, Takatsuki, et al., 2008;  
180 Watari, Nishijima, et al., 2013). To avoid such a situation, it would have been  
181 necessary to sufficiently increase the killing rate and specific killing rate, as  
182 shown in (Fig. 2: bottom left). When  $\alpha = 1$  (control is very low) or  $\alpha = 3$

183 (control is sufficiently high), the final results do not differ between model (2)  
 184 and model (12), but a large difference is observed when  $\alpha = 2$ . In this case,  
 185 model (2) suggests extinction of native species (Fig. 2: middle left), but  
 186 model (12) indicates survival of native species and overestimates the effect  
 187 of control (Fig. 2: middle right), because it ignores the initial growth of  
 188 invasive species by predation. As can be seen from this example, when using  
 189 the model (12), it is essential to check if the assumptions  $i_2 \sim 0$  and  $j_2 \sim 0$   
 190 are sufficiently valid to ensure that the estimates do not differ significantly  
 191 from the real system.

192 The results of this study suggest the parameters that should be prioritized  
 193 for estimation (Fig. 3). We should start by measuring the intrinsic growth  
 194 rate,  $r_1, r_2$ , and the specific killing rate  $\alpha$ . Based on these parameters and  
 195 inequality (6), we can determine whether the control program eradicates  
 196 only invasive species. Next, it is recommended to estimate the interaction  
 197 coefficients of the native species  $i_1, j_1$  and killing rate  $c$ . These parameters,  
 198 along with  $r_1, r_2$ , allow us to understand the approximate dynamics of the  
 199 system by the model (12). Then, when we obtain the intraspecific coefficient  
 200 of the invasive species,  $i_2$ , we can use the condition (5) to determine whether  
 201 the system exists in state (a), and whether eradication is urgently needed.  
 202 Finally, if the interspecific coefficient of the invasive species  $j_2$  is acquired, it  
 203 is possible to set detailed goals using the model (2) and bycatch curve (9).

204 In mathematical modeling studies, control of invasive species can lead  
 205 to counterintuitive results (Courchamp, Langlais, et al., 1999; Courchamp,

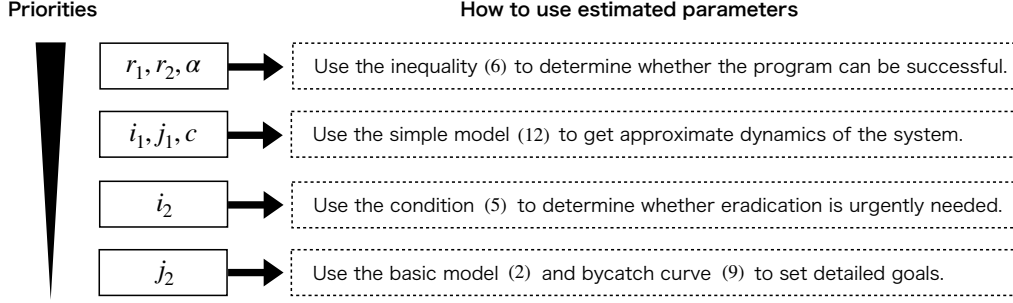


Figure 3: Parameters to be prioritized for estimation.  $r_1, r_2$  are the intrinsic growth rates,  $i_1, i_2$  are the intraspecific interaction coefficients,  $j_1, j_2$  are the interspecific interaction coefficients,  $c$  is the killing rate of native species, and  $\alpha$  is the specific killing rate of invasive species. Subscripts 1 and 2 denote native and invasive species, respectively.

Langlais, et al., 2000; Caut et al., 2007). Therefore, it is important to identify the characteristic interactions among species and model them in a flexible manner. For example, if secondary poisoning is a concern, it may be necessary to use a model that takes into account predators of higher trophic levels than the invasive species. In addition, if the invasive species is an opportunistic predator or its spatial distribution is not uniform, the interaction term must be improved. A descriptive approach using food webs is useful to identify interactions among species (Innes & Barker, 1999).

To resolve concerns about bycatch, it is necessary to prove the validity of the control plan with sufficient evidence. Therefore, we hope that the results of this study will not be used independently, but in combination with experimental data.

## 218 Declaration of competing interest

219 The author has no competing interest directly relevant to the content of  
220 this article.

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