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# **Void Fraction and Interfacial Friction in Vertical Circular Pipes with the Square Top End under Flooding Conditions**

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## Abstract

*The objective of this study was to reduce the uncertainties of correlations for flow characteristics in vertical pipes under flooding at the top end. The void fraction  $\alpha$ , pressure gradient  $dP/dz$ , and countercurrent flow limitation (CCFL) were previously measured with diameter  $D = 40$  mm and working fluid of air and water. The wall friction and interfacial friction factors ( $f_w$  and  $f_i$ ) were obtained based on the annular flow model, and CCFL and  $f_w$  were evaluated in detail. Hence evaluations of  $\alpha$  and  $f_i$  were turned out attention in detail. The liquid film thickness  $\delta$  and  $f_i$  for the smooth film (SF) due to flooding at the top end were obtained by using the previously derived  $f_w$  correlation and existing  $dP/dz$  data with  $D = 20$ - $50.8$  mm and pressure  $P = 0.1$ - $4.1$  MPa, and empirical correlations for  $\delta$  and  $f_i$  were derived.  $\delta$  was well expressed by a function of the liquid Reynolds number  $Re_L$ , and the uncertainty of the  $\delta$  correlation was  $\pm 0.0062$  for  $\alpha = 0.87$ - $0.98$ .  $f_i$  was expressed by a function of  $\delta/L$  (where  $L$  is the Laplace length) or the Kutateladze parameter  $K_G^*$ , the dimensionless diameter  $D^*$  ( $= D/L$ ), and the density ratio of gas and liquid phases  $\rho_G/\rho_L$ . The applicability of the derived correlations to conditions of  $D = 300$  mm and  $P = 7$  MPa was evaluated, and the  $f_i$  correlation was modified based on  $f_i$  values computed with the  $\delta$  correlation. The drift-flux parameters for SF were also considered.*

## I. INTRODUCTION

In an accident analysis for light water reactors such as a pressurized water reactor (PWR) and a boiling water reactor (BWR), models and correlations for flow characteristics under flooding conditions are important to evaluate the pressure loss and

the distribution of the coolant mass in the system. The objective of this study was to reduce uncertainty of correlations for countercurrent flow limitation (CCFL), the void fraction  $\alpha$ , the wall friction factor  $f_w$ , and the interfacial friction factor  $f_i$  under flooding conditions, which are used in an accident analysis. While many flooding studies have been done,<sup>1,2</sup> flow characteristics in vertical pipes under flooding conditions depend on the top and bottom end shapes, and the characteristics are not well understood mainly due to lack of data for  $\alpha$ . Bharathan et al.<sup>3</sup> measured CCFL (i.e. relationship between the time-averaged superficial gas and liquid velocities  $J_G$  and  $J_L$ ), pressure gradient  $dP/dz$ , and the liquid film thickness  $\delta$  in vertical pipes, and obtained  $f_w$  and  $f_i$  under flooding conditions based on the annular flow model. They classified the liquid film as the rough film (RF) due to flooding at the bottom end and as the smooth film (SF) due to flooding at the top end.  $\delta$  was under-detected for large  $\delta$  and the obtained  $f_w$  was sometimes negative. Subsequently, Bharathan et al.<sup>4</sup> and Bharathan and Wallis<sup>5</sup> obtained  $f_i$  from the measured  $dP/dz$  by assuming  $f_w = 0$ , and proposed an  $f_i$  correlation for RF. However, they offered little discussion on SF. Figure 1 illustrates the top and bottom end shapes in a vertical pipe and the flow patterns under flooding conditions. The flow patterns depend on the relationship between the falling liquid flow rates limited by flooding at the top and bottom ends  $W_{L,T}$  and  $W_{L,B}$ . The bottom end shape of the heat transfer tubes in a steam generator is square, and the top end shape of the pressurizer surge line is square.

In our research group, Goda et al.<sup>6</sup> measured CCFL,  $dP/dz$  and  $\alpha$  by using quick closing valves in vertical pipes (diameter of  $D = 20$  and  $40$  mm; the rounded top end and square (i.e. sharp-edged without curvature) bottom end; working fluid of air and water), and obtained  $f_w$  and  $f_i$ . Shimamura et al.<sup>7</sup> and Takaki et al.<sup>8</sup> carried out similar experiments to Goda et al.<sup>6</sup> with the square top end and rounded bottom end, and working fluid of air and water for  $D = 20$  mm and  $40$  mm, respectively, and they obtained  $f_w$  and  $f_i$ . Table I

lists their experimental conditions<sup>6,7,8</sup> in comparison with those by Bharathan et al.<sup>3</sup> and Ilyukhin et al.<sup>9</sup> Bharathan et al.<sup>3</sup> measured  $\delta$  but uncertainty for the measurement was large. Ilyukhin et al.<sup>9</sup> did not measure  $\alpha$  but measured  $dP/dz$ . Takaki et al.<sup>8</sup> previously evaluated CCFL characteristics and  $f_w$  for SF in detail, because they are important to obtain  $\alpha$  and  $f_i$  from the  $dP/dz$  data. However, evaluation of  $\alpha$  (or  $\delta$ ) and  $f_i$  remained to be an unresolved subject.

The objective of this paper was to obtain  $\alpha$  and  $f_i$  for SF flooding at the square top end by using the  $f_w$  correlation proposed by Takaki et al.<sup>8</sup> and existing  $dP/dz$  data and to derive their correlations, which can be used in an accident analysis up to 7 MPa steam-water conditions. To evaluate features of flow characteristics for RF and SF, we firstly compared the data by Goda et al.<sup>6</sup> for  $D = 40$  mm with the square bottom end and the data by Takaki et al.<sup>8</sup> for  $D = 40$  mm with the square top end. Then, we obtained  $\alpha$  and  $f_i$  from  $dP/dz$  data reported by Bharathan et al.<sup>3</sup> and Ilyukhin et al.,<sup>9</sup> and we derived empirical correlations for  $\delta$  and  $f_i$  for SF by using data listed in Table I. The water level  $h$  in the upper tank affects CCFL characteristics.<sup>10,11</sup> Bharathan et al.<sup>3</sup> classified  $h$  to  $h > 2D$  and  $h < D$ , and we used data with  $h > 2D$ . Ilyukhin et al.<sup>9</sup> did not report the  $h$  values, and we judged that  $h$  was high from the experimental setup drawing. Takaki et al.<sup>12</sup> showed that  $\alpha$  and  $f_i$  could be accurately obtained from the  $dP/dz$  data and a reliable  $f_w$  correlation by using the annular flow model. We also examined the drift-flux parameters (Zuber and Findlay<sup>13</sup>) for SF, because the drift flux model is used in some accident analysis codes. We finally evaluated applicability of the derived correlations to large diameter ( $D = 0.3$  m which is the diameter of the pressurizer surge line in a PWR) and high pressure ( $P = 7$  MPa) steam-water conditions.

## II. EVALUATION METHOD AND FLOW CHARACTERISTICS UNDER FLOODING CONDITIONS

### II.A. Annular Flow Model and Flow Patterns

In the annular flow model, the force balance equations for the gas core and the entire cross section are expressed in dimensionless forms as:<sup>5,6,8,12</sup>

$$\left(\frac{dP}{dz}\right)^* + \frac{\rho_G}{\rho_L - \rho_G} + \left(\frac{2f_i}{\alpha^{1/2}}\right) \left\{ \frac{J_G^*}{\alpha} - \left(\frac{\rho_G}{\rho_L}\right)^{1/2} \frac{J_L^*}{1-\alpha} \right\}^2 = 0, \quad (1)$$

and

$$\left(\frac{dP}{dz}\right)^* + \left\{ (1-\alpha) + \frac{\rho_G}{\rho_L - \rho_G} \right\} - 2f_w \left( \frac{J_L^*}{1-\alpha} \right)^2 = 0, \quad (2)$$

where

$$J_i^* = \frac{J_i}{[gD(\rho_L - \rho_G)]^{1/2} \rho_i} \quad (i = G \text{ or } L) \quad (3)$$

and

$$\left(\frac{dP}{dz}\right)^* = \frac{dP/dz}{(\rho_L - \rho_G)g}.$$

(4)

Additionally, here  $D$  is the diameter,  $f_i$  is the interfacial friction factor,  $f_w$  is the wall friction factor,  $g$  is the gravitational acceleration,  $J$  is the superficial velocity,  $J^*$  is the Wallis parameter,  $P$  is the pressure,  $z$  is the vertical coordinate,  $\alpha$  is the void fraction, and  $\rho$  is the density. The subscripts  $G$  and  $L$  denote the gas and liquid phases, respectively.  $J_G > 0$  for the upward flow of the gas phase, while  $J_L < 0$  for falling liquid motion. We can obtain  $f_i$  and  $f_w$  from Eqs. (1) and (2), respectively, by measuring CCFL ( $J_L$  for a given  $J_G$ ),  $dP/dz$ , and  $\alpha$ .

Figure 2 (a) shows flow characteristics (the liquid volume fraction  $(1-\alpha)$ ,  $|dP/dz|^*$

and  $J_L^*$ ) in a vertical pipe with  $D = 20$  mm, and the square top and rounded bottom ends under flooding conditions reported by Shimamura et al.<sup>7</sup> All flow patterns of SF, TR (transition from SF to RF) and RF appeared in the experiments. Figure 2 (b) shows the time-strip images,<sup>7</sup> where the gray values of pixels along the pipe axis were extracted from each image taken by using a high-speed video camera with the frame rate of 350 fps and were rearranged in the horizontal direction. In the region of  $J_G < 5.9$  m/s,  $J_L$  was limited at the top end as shown in Fig. 1 (b) and the relatively smooth film (SF) formed in the vertical pipe. However, the downward motion of interfacial waves were observed even in SF due to intermittent liquid inflow at the top end. In the region of  $5.9 \text{ m/s} < J_G < 7.4 \text{ m/s}$  (where the flow pattern was TR), the disturbance waves appeared due to flooding near the bottom end, and  $J_L$  was limited at the top and bottom ends simultaneously (see Fig. 1 (b)). The disturbance waves did not reach to the upper tank. In the region of  $J_G > 7.4 \text{ m/s}$ , the disturbance waves flew up to the upper tank in RF.  $(1-\alpha)$  decreases with increasing  $J_G$  in SF and RF but increases with increasing  $J_G$  in TR depending on the heights of regions for RF and SF (see Fig. 1 (b) and Fig. 2 (b)). In Eqs. (1) and (2),  $\rho_G/(\rho_L - \rho_G) \ll 1$ . Hence  $|dP/dz|^*$  is nearly equal to the  $f_i$  term or the difference between  $(1-\alpha)$  and the  $f_w$  term.

The diameter and shapes at the top and bottom ends affected  $J_G$  at the flow pattern transition.<sup>6,8</sup> In the vertical pipe with  $D = 20$  mm, and the rounded top and square bottom ends (R/S),<sup>6</sup> the disturbance waves at the bottom end occurred at low  $J_G$ , and the flow pattern was RF in the region of  $J_G > 2.5$  m/s. This was because flooding at the square bottom end occurred at low  $J_G$ .

## II.B. CCFL Characteristics

The Wallis CCFL correlation<sup>1</sup> defined by Eq. (5) is widely used in accident analysis codes to compute  $J_L$  for a given  $J_G$  under flooding conditions.

$$J_G^{*1/2} + m |J_L|^{*1/2} = C, \quad (5)$$

where  $C$  and  $m$  are empirical constants. Kusunoki et al.<sup>14</sup> proposed Eq. (6) for flooding at the bottom end.

$$\begin{aligned} \frac{J_G^{*1/2}}{(\mu_G / \mu_L)^{0.07}} = & (1.04 \pm 0.05) - 3.6 \left\{ \left( \frac{\mu_G}{\mu_L} \right)^{0.1} |J_L|^{*1/2} \right\} + 11 \left\{ \left( \frac{\mu_G}{\mu_L} \right)^{0.1} |J_L|^{*1/2} \right\}^2 \\ & - 16 \left\{ \left( \frac{\mu_G}{\mu_L} \right)^{0.1} |J_L|^{*1/2} \right\}^3 \quad (14 \text{ mm} \leq D \leq 51 \text{ mm}) \end{aligned} \quad (6)$$

Eq. (6) was modified to the Wallis correlation (i.e. a linear function of  $J_G^{*1/2}$  and  $|J_L|^{*1/2}$ ) for an accident analysis,<sup>15</sup> but its uncertainty was large due to the effect of fluid properties. Murase et al.<sup>11</sup> proposed Eq. (7) with the Kutateladze parameters  $K_i^*$  for flooding at the top end.

$$K_G^{*1/2} + 0.97 |K_L|^{*1/2} = 1.53 \pm 0.11 \quad (11 \leq D^* \leq 94), \quad (7)$$

where

$$\begin{aligned} K_i^* &= D^{*1/2} J_i^* \\ &= \frac{J_i}{\{\sigma g (\rho_L - \rho_G) / \rho_i^2\}^{1/4}} \quad (i = G \text{ or } L) \end{aligned} \quad (8)$$

$$D^* = \frac{D}{L}, \quad (9)$$

$$L = \left\{ \frac{\sigma}{(\rho_L - \rho_G)g} \right\}^{1/2}, \quad (10)$$

where  $L$  is the Laplace length and  $\sigma$  is the surface tension.

Figure 3 shows CCFL characteristics with  $D = 40$  mm, and the square top and rounded bottom ends (S/R)<sup>8</sup> and the rounded top and square bottom ends (R/S).<sup>6</sup> In both



cases, flooding occurred near the top end and falling liquid formed SF in the region of low  $J_G$ ; with increasing  $J_G$ , the SF was further changed in the transition region (TR: where flooding occurred near the top and bottom ends simultaneously).  $J_L$  was larger for R/S than for S/R due to the rounded top end for SF, but  $J_L$  became similar in both cases for the TR even though there was a different shape at the bottom end.  $C_W = (1.04 \pm 0.05) (\mu_G/\mu_L)^{0.07} = 0.79 \pm 0.038$  for air-water in Eq. (6) and  $C_W = (1.53 \pm 0.11)/D^{*1/4} = 0.78 \pm 0.056$  for  $D = 40$  mm in Eq. (7). The difference between values obtained by Eqs. (6) and (7) was small.  $J_L^*$  measured with S/R agreed well with Eq. (6) for R/S except in the region of small  $J_G^*$ .  $J_L^*$  for S/R was lower than the mean value of Eq. (7) for S/R in the region of large  $J_G$ , but was within the uncertainty of  $\pm 0.11$  in Eq. (7).

The slope  $m$  in Eq. (5) was larger for S/R except in the region of large  $J_G^*$  than for R/S, and this was the cause of flooding near the top end at low  $J_G^*$  and near the bottom end at medium to larger  $J_G^*$ . The transition point from SF to TR may be given by the intersection of CCFL curves near the top end and near the bottom end.

## II.C. Void Fraction and Pressure Gradient

Figure 4 shows  $(1-\alpha)$  and  $-(dP/dz)^*$  defined by Eq. (4) for S/R<sup>8</sup> and R/S.<sup>6</sup> The difference between  $(1-\alpha)$  and  $-(dP/dz)^*$ , i.e.  $(1-\alpha) + (dP/dz)^*$ , nearly equals the  $f_w$  term, because  $\rho_G/(\rho_L - \rho_G)$  is very small in Eq. (2). At the largest  $J_G$  for S/R, the occurrence of TR or RF was not clear from a visual observation.  $(1-\alpha)$  and  $-(dP/dz)^*$  differed between S/R and R/S due to the different flow structure. The  $f_w$  term was large for SF and small for RF. Bharathan and Wallis<sup>5</sup> neglected the  $f_w$  term for RF. They indicated that the  $f_w$  term for SF cannot be neglected, but they did not propose a correlation for  $f_w$  in SF. For S/R, the TR region was broad. SF, TR and RF are for classification of flow structure shown by Bharathan and Wallis,<sup>5</sup> and the gas-liquid interface in SF is not actually smooth due to interfacial waves caused by intermittent liquid inflow at the top end (see Fig. 2

(b)).<sup>8</sup>

Even for SF at small  $J_G^*$ ,  $(1-\alpha)$  and  $-(dP/dz)^*$  were larger for R/S than those for S/R due to the larger  $J_L$  (see Fig. 3). In the region of large  $J_G^*$  ( $> 0.5$ ),  $(1-\alpha)$  and  $-(dP/dz)^*$  were larger for S/R than they were for R/S, and the reason of this was not clear. In the region of medium  $J_G^*$ , where it was larger than  $J_G^*$  at the transition point from SF to TR for S/R ( $J_G^* = 0.26$ ,  $J_G = 4.7$  m/s),  $J_L^*$  was almost the same between S/R and R/S as shown in Fig. 3, but  $(1-\alpha)$  and  $-(dP/dz)^*$  were much smaller for S/R than they were for R/S due to the differences of the shape of the bottom end (square or rounded) and formation of disturbance waves there.

It is well known that  $J_L^*$  is the largest with the rounded top and bottom ends (R/R) among combinations of the top and bottom end shapes shown in Fig. 1 (a),<sup>1,2</sup> but reliable  $\alpha$  data in vertical pipes with R/R are not found. Measurement of  $\alpha$  with R/R is remains as future work.

## II.D. Wall Friction Factor

$(dP/dz)^*$  and  $\alpha$  data are needed to obtain  $f_w$  from Eq. (2), but  $\alpha$  data under flooding conditions are limited. Therefore,  $f_w$  for single-phase flows is widely used,<sup>12,16</sup> and the  $f_w$  correlation is expressed by:

$$f_w = \max\left(\frac{16}{Re_L}, \frac{0.079}{Re_L^{0.25}}\right), \quad (11)$$

$$Re_L = \frac{|J_L|D}{\nu_L}, \quad (12)$$

where  $Re_L$  is the liquid Reynolds number and  $\nu$  is the kinematic viscosity. Takaki et al.<sup>8</sup> proposed a  $f_w$  correlation ( $f_w = 0.70/Re_L^{0.50}$ ) for the transition region between laminar and turbulent flows, and they speculated that the correlation could be combined with Eq. (11),

i.e.:

$$f_w = \max \left( \frac{16}{Re_L}, \frac{0.70}{Re_L^{0.50}}, \frac{0.079}{Re_L^{0.25}} \right). \quad (13)$$

Figure 5 shows  $f_w$  for S/R<sup>8</sup> and R/S<sup>6</sup> as a function of  $Re_L$ .  $f_w$  was obtained from Eq. (2) by using the measured CCFL ( $J_L$  for given  $J_G$ ),  $dP/dz$ , and  $\alpha$ .  $f_w$  for SF was expressed well by Eq. (13). In the laminar flows for  $D = 40$  mm,  $f_w$  for both S/R and R/S was well expressed by the correlation proposed by Goda et al.:<sup>6</sup>

$$f_w = \frac{28600}{Re_L^{1.96}}. \quad (14)$$

The liquid downward and upward flows due to the flooding near the bottom end and formation of disturbance waves in TR and RF increased the velocity gradient near the wall, and this increased  $f_w$ . Figure 5 suggested that the liquid velocity distribution near the wall would be similar between TR for S/R and RF for R/S in  $D = 40$  mm.

## II.E. Interfacial Friction Factor

The  $f_i$  can be computed by using Eq. (1), empirical correlations for  $J_L$  and  $f_w$  (Eqs. (7) and (13) for SF for example), and a correlation for  $\alpha$ . However, a correlation for  $f_i$  is sometimes used in accident analysis codes. Bharathan and Wallis<sup>5</sup> proposed a correlation for  $f_i$  derived from  $dP/dz$  data for RF reported by Bharathan et al.:<sup>4</sup>

$$\begin{aligned} f_i &= 0.005 + A \left( \frac{\delta}{L} \right)^B, \\ \log_{10} A &= -0.56 + \frac{9.07}{D^*}, \\ B &= 1.63 + \frac{4.74}{D^*}. \end{aligned} \quad (15)$$

Sano et al.<sup>17</sup> proposed an  $f_i$  correlation for RF by using previously reported data.<sup>4,6</sup> The  $f_i$  correlation for air-water conditions was expressed by:

$$f_i = 0.30D^* \exp(-1.90K_G^*). \quad (16)$$

The form of Eq. (16) is simple in comparison with Eq. (15). Both Eqs. (15) and (16) are for RF. On the other hand, a suitable  $f_i$  correlation for SF has not been proposed.

Figure 6 shows  $f_i$  for S/R<sup>8</sup> and R/S.<sup>6</sup>  $f_i$  was obtained from Eq. (1) by using the measured CCFL ( $J_L$  for given  $J_G$ ),  $dP/dz$ , and  $\alpha$ .  $f_i$  differed between S/R and R/S due to the different  $(1-\alpha)$  (see Fig. 4). Eqs. (15) and (16) were derived for RF, but Eq. (15) underestimated  $f_i$  except for the region of large  $J_G$ . In TR of S/R,  $f_i$  increased and decreased with increasing  $J_G$  (we expected a narrow region for TR and simple increase of  $f_i$  with increasing  $J_G$ ). The reason for this complex change in  $f_i$  was not clear, but might be due to unstable generation of disturbance waves near the rounded bottom end. The  $f_i$  value at large  $J_G$  was larger for S/R than that for R/S (we expected RF occurrence and similar  $f_i$  values for S/R and R/S at large  $J_G$ ).

### III. LIQUID FILM THICKNESS AND INTERFACIAL FRICTION FOR SMOOTH FILM

Takaki et al.<sup>8</sup> evaluated CCFL characteristics and  $f_w$  for SF due to flooding at the top end in detail, but did not discuss  $\alpha$  (or  $\delta$ ) and  $f_i$  in detail. In this section, therefore, we obtained  $\delta$  and  $f_i$  by using the  $f_w$  correlation reported by Takaki et al.<sup>8</sup> and  $dP/dz$  data reported by Bharathan et al.<sup>3</sup> and Ilyukhin et al.,<sup>9</sup> and we discussed  $\delta$  and  $f_i$  for SF in detail.

#### III.A. Liquid Film Thickness

The relationship between  $\alpha$  and  $\delta$  in the annular flow can be expressed by:

$$\alpha = \left(1 - \frac{2\delta}{D}\right)^2 \quad \text{or} \quad \frac{\delta}{D} = \frac{1 - \alpha^{1/2}}{2}. \quad (17)$$

Kamei et al.<sup>18</sup> were the first to measure  $\delta$  with the weighting method under flooding conditions, and they showed  $\delta$  under flooding conditions was thicker than  $\delta$  for the free falling film. However, uncertainty of their measurements was large. Feind<sup>19</sup> and Hewitt and Wallis<sup>20</sup> measured  $\delta$  under countercurrent flow conditions just before the onset of flooding or formation of laminar liquid films and found  $\delta$  under countercurrent flow conditions was similar to  $\delta$  for the free falling film. Therefore, Nusselt's equation<sup>21</sup> for laminar flows in free falling films is widely used for  $\delta$  in SF. Imura et al.<sup>22</sup> used Feind's experimental equation<sup>19</sup> for turbulent flows to compute  $\alpha$  under flooding conditions. The combination of Nusselt's equation and Feind's experimental equation is given by:

$$\frac{\delta}{L_v} = \max \left\{ \left( \frac{3Re_L}{4} \right)^{1/3}, 0.266Re_L^{1/2} \right\}, \quad (18)$$

$$L_v = \left( \frac{v_L^2}{g} \right)^{1/3}. \quad (19)$$

Takaki et al.<sup>12</sup> obtained  $\alpha$  by using Eq. (2), a correlation for  $f_w$ , and the  $(dP/dz)^*$  and CCFL data by Bharathan et al.<sup>3</sup> with  $D = 50.8$  mm and air-water and by Ilyukhin et al.<sup>9</sup> with  $D = 20$  mm and steam-water at  $P = 0.6$ -4.1 MPa, and they proposed a  $\delta$  correlation for turbulent flows. The correlation for turbulent flows in Eq. (18) was replaced as:

$$\frac{\delta}{L_v} = \max \left\{ \left( \frac{3Re_L}{4} \right)^{1/3}, 0.091Re_L^{0.64} \right\}. \quad (20)$$

Figure 7 shows  $\delta/L_v$  for S/R<sup>8</sup> and R/S<sup>6</sup> with  $D = 40$  mm. For a  $J_G^*$  value,  $(1-\alpha)$  for SF was larger for R/S than that for S/R as shown in Fig. 4, but the relationship between  $\delta/L_v$  and  $Re_L$  for SF was close between S/R and R/S as shown in Fig. 7 because  $J_L^*$  (i.e.

$Re_L$ ) for SF was larger for R/S than that for S/R as shown in Fig. 3. The  $\delta/L_v$  data by Shimamura et al.<sup>7</sup> with  $D = 20$  mm are shown only for SF. Eq. (20) for SF proposed by Takaki et al.<sup>12</sup> underestimated  $\delta$  in the transition region between laminar and turbulent flows.

Many  $\delta$  correlations for the free falling films have been proposed as the form of  $\delta/L_v = a Re_L^n$ , where  $n = 1/3$  for the laminar flow.<sup>21</sup> Several  $n$  values have been proposed for the turbulent flow and they are  $n = 0.6$  and  $2/3$ ,<sup>1</sup>  $n = 2/3$ ,<sup>23</sup>  $n = 8/15$ ,<sup>24</sup> and  $n = 1/2$ <sup>19</sup> depending on the database. In this study, we redetermined  $\alpha$  by using Eq. (2), Eq. (13), and  $(dP/dz)^*$  and CCFL data by Bharathan et al.<sup>3</sup> and by Ilyukhin et al.<sup>9</sup> We derived  $\delta$  correlations for the transition and turbulent regions by using our  $\alpha$  data and the redetermined  $\alpha$ . We used the form of  $\delta/L_v = a Re_L^n$ , and  $n = 1/2$  for the transition region and  $n = 2/3$  for the turbulent region, and we obtained the  $a$  value as the average in the ranges of  $1000 < Re_L < 3000$  and  $Re_L > 3000$  for the transition and turbulent regions, respectively. The derived correlation was expressed by:

$$\frac{\delta}{L_v} = \max \left\{ \left( \frac{3Re_L}{4} \right)^{1/3}, 0.32Re_L^{1/2}, 0.076Re_L^{2/3} \right\}. \quad (21)$$

Figure 8 compares Eq. (21) with data for (a)  $\delta/L_v$  and (b)  $\alpha$ . In the computation of  $(1-\alpha)$  with Eq. (2), the maximum difference between Eqs. (11) and (13) for  $f_w$  was 0.0045 at  $Re_L = 1300$  and its effect on  $\delta$  was 12 %. The  $\delta$  value by Eq. (21) was 133 % of the  $\delta$  value by Eq. (18) at  $Re_L = 10000$ . The uncertainty of  $\pm 0.0062$  for the void fraction included 95 % of the data points. This showed that Eq. (21) gave good agreement with  $\alpha$  data.

### III.B. Interfacial Friction Factor

To evaluate  $f_i$ , accurate measurement of  $dP/dz$  is needed, because  $f_i$  is in proportion

to  $-dP/dz$  as expressed by Eq. (1) and  $-dP/dz$  for SF is small as shown in Fig. 4. On the other hand, the effect of uncertainty in the  $\alpha$  evaluation is relatively small because  $\alpha$  is relatively large.

Figure 9 shows  $f_i$  evaluated from  $dP/dz$  data reported by Bharathan et al.<sup>3</sup> In the region of  $J_G^* > 0.5$  (where  $J_L = 0$ ), flooding occurred near the rounded bottom end, and  $-dP/dz$  and  $(1-\alpha)$  increased. In the region of SF (where  $J_G^* < 0.5$ ),  $-dP/dz$  was small and its change with increasing  $J_G$  was small. This made uncertainty for  $f_i$  large. The  $f_i$  values reported by Bharathan et al.<sup>3</sup> were large at small  $J_G^*$  as shown in Fig. 9, because they neglected the  $J_L/(1-\alpha)$  term in Eq. (1) assuming  $|J_L|/(1-\alpha) \ll J_G/\alpha$ . Figure 9 showed that the  $f_i$  values computed with Eqs. (1), (2) and (13) and  $dP/dz$  data (where  $J_L^*$  measured for a given  $J_G^*$  was used) agreed well with the  $f_i$  values obtained from  $dP/dz$  and  $\delta$  data and Eq. (1). This was due to the small effect of the  $\alpha$  value on  $f_i$ .

Figure 10 shows  $f_i$  evaluated from  $dP/dz$  data reported by Ilyukhin et al.<sup>9</sup> Dispersion of  $dP/dz$  data reported by Ilyukhin et al.<sup>9</sup> was large compared with data reported by Shimamura et al.<sup>7</sup> This large dispersion led to the large dispersion for the  $f_i$  value in Fig. 10, which was computed with Eqs. (1), (2) and (13) and  $dP/dz$  data. The  $f_i$  value by Shimamura et al.<sup>7</sup> was obtained from  $dP/dz$  and  $\alpha$  data and Eq. (1).

For RF, Sano et al.<sup>17</sup> proposed Eq. (16) as a function of  $K_G^*$ . The constant  $A$  and exponent  $B$  for  $f_i = A K_G^{*B}$  were obtained for each experiment by using the least square method, and  $A$  and  $B$  were expressed by functions of  $D^*$  and the density ratio of gas and liquid phases  $\rho_G/\rho_L$ . As a result, we derived the following  $f_i$  correlation.

$$f_i = A K_G^{*B},$$

$$A = \left( \frac{9.0}{10^5} \right) \left( \frac{\rho_L}{\rho_G} \right)^{0.60} D^*,$$

$$B = \frac{-25 (\rho_G / \rho_L)^{0.25}}{D^{*0.50}} \quad \text{for } 7.8 \leq D^* \leq 18.6. \quad (22)$$

Figure 11 shows effects of (a) diameters and (b) fluid properties on  $f_i$  for SF as a function of  $\delta/L$ , which is used in Eq. (15). From  $A$  and  $B$  for  $f_i = A (\delta/L)^B$  shown in Fig. 11,  $A$  and  $B$  were expressed by functions of  $D^*$  and  $\rho_G/\rho_L$ , and we derived the following  $f_i$  correlation.

$$f_i = A \left( \frac{\delta}{L} \right)^B,$$

$$A = \frac{260 (\rho_L / \rho_G)^{0.35}}{D^{*2.9}},$$

$$B = \frac{11.4}{D^{*0.73}} \quad \text{for } 7.8 \leq D^* \leq 18.6. \quad (23)$$

Figure 12 (a) and (b) compare  $f_{i,c}$  values computed with the derived correlations, Eqs. (22) and (23), with the measured  $f_{i,m}$ , respectively. In Fig. 12 (a), Eq. (22) underestimated  $f_i$  for  $D = 40$  mm, but overestimated  $f_i$  for  $D = 50.8$  mm. On the other hand, in Fig. 12 (b), Eq. (23) gave good agreement with  $f_{i,m}$ . Figure 12 showed that Eq. (23) was better than Eq. (22) for a  $f_i$  correlation.

### III.C. Drift-Flux Parameters

In Eqs. (1) and (2),  $J_G^*$  is generally a given condition,  $J_L^*$  is obtained from a CCFL correlation, and  $\alpha$  and  $(dP/dz)^*$  are solved by using correlations for  $f_w$  and  $f_i$ . In some accident analysis codes, the drift-flux model proposed by Zuber and Findlay<sup>13</sup> is used instead of the  $f_i$  correlation. The general expression of the one-dimensional drift-flux model is:

$$\frac{\langle J_G \rangle}{\langle \alpha \rangle} = C_0 \langle J \rangle + V_{gj}, \quad (24)$$



$$\langle J \rangle = \langle J_G + J_L \rangle, \quad (25)$$

where  $\langle J_G \rangle$  is the area-averaged superficial gas velocity,  $\langle J \rangle$  is the area-averaged mixture volumetric flux,  $\langle \alpha \rangle$  is the area-averaged void fraction,  $C_0$  is the distribution parameter, and  $V_{gj}$  is the drift velocity.

Figure 13 shows the drift-flux plots for SF with working fluids of (a) air-water and (b) steam-water.  $C_0 = 1$  was a good approximation for all cases due to the reason of annular flows. Figure 14 shows the dimensionless drift velocity  $V_{gj}^*$  ( $= V_{gj} / [\sigma \cdot g \cdot (\rho_L - \rho_G) / \rho_L^2]^{1/4}$ ) with the approximation of  $C_0 = 1$  for SF with working fluids of (a) air-water and (b) steam-water.  $V_{gj}^*$  was about 2.0 for S/R in the mid gas velocity of  $K_G^* = 0.5-1$  and  $V_{gj}^*$  decreased with increasing  $K_G^*$ .  $V_{gj}^*$  for S/S was smaller than  $V_{gj}^*$  for S/R.  $V_{gj}^*$  for high pressure steam-water was 0.7-1.1 and was smaller than  $V_{gj}^*$  for air-water. From Fig. 14, the correlations for the drift-flux parameters ( $C_0$  and  $V_{gj}$ ) were expressed by:

$$C_0 = 1, \quad (26)$$

$$V_{gj}^* = \min \left[ \frac{\max \{ 0.014 (\rho_L / \rho_G)^{0.74}, 0.76 \}}{K_G^{*0.37}}, 2.0 \right] \quad \text{for } 7.8 \leq D^* \leq 18.6, \quad (27)$$

$$V_{gj}^* = \frac{V_{gj}}{\{ \sigma \cdot g \cdot (\rho_L - \rho_G) / \rho_L^2 \}^{1/4}}, \quad (28)$$

where the density ratio of gas and liquid phases  $\rho_G / \rho_L$  was used. The restricted values of 0.76 and 2.0 were for high pressure and small  $K_G^*$ , respectively. When the viscosity ratio of gas and liquid phases  $\mu_G / \mu_L$  was used, the correlation for  $V_{gj}^*$  with  $C_0 = 1$  was expressed by:

$$V_{gj}^* = \min \left[ \frac{\max \{ 0.26 (\mu_L / \mu_G)^{0.50}, 0.76 \}}{K_G^{*0.37}}, 2.0 \right] \quad \text{for } 7.8 \leq D^* \leq 18.6. \quad (29)$$

Figure 15 compares  $\alpha_c$  computed with Eqs. (24), (26) and (27) or (29) with the measured  $\alpha_m$ . The uncertainty, which included 95 % of the data points, was  $\pm 0.015$  for (a) Eqs. (24), (26) and (27) and  $\pm 0.013$  for (b) Eqs. (24), (26) and (29). The difference between  $\alpha_c$  and  $\alpha_m$  was relatively large in comparison with  $\pm 0.0062$  for Eq. (21) shown in Fig. 8 (b).

#### IV. EFFECTS OF DIAMETER AND FLUID PROPERTIES

Our target for the derived correlations was to apply them to an accident analysis for a small-break loss-of-coolant accident in a PWR, where the maximum vertical pipe is about 0.3 m in the diameter for the pressurizer surge line and the highest pressure for two-phase flows in the primary loop may be mainly up to 7 MPa. The maximum value for the dimensionless diameter is  $D^* = D/L = 187$  at 7 MPa for  $D = 0.30$  m.

Eq. (7) for CCFL characteristics was derived from data of  $D^* \leq 94$ . Existing CCFL data for vertical pipes show that the CCFL constant  $C_K$  with the Kutateladze parameters like Eq. (7) approaches a constant value with increasing  $D^*$ .<sup>5,11,25,26</sup> Therefore, Eq. (7) for vertical pipes may be applied up to  $D^* = 187$ . Eq. (13) for  $f_w$  may be applied up to  $D^* = 187$  because it is basically based on the correlation for single-phase flows.

##### IV.A. Correlation for Liquid Film Thickness

Applicability of Eq. (21) for  $\delta$  to large  $D^*$  was not clear, hence we evaluated its rationality to large  $D^*$ . Figure 16 shows  $\delta$  values calculated by Eq. (21) for effects of (a)  $D$  and (b)  $P$  (i.e. fluid properties). There are no data to confirm validity of the calculated values, but they did not show unreasonable trends.

##### IV.B. Correlation for Interfacial Friction Factor

It seems that Eqs. (7) for CCFL, (13) for  $f_w$  and (21) for  $\delta$  may be applied up to  $D^* = 187$  ( $D = 0.3$  m and  $P = 7$ MPa). We can calculate  $dP/dz$  and  $f_i$  by using the

momentum equations of Eqs. (1) and (2) and the correlations of Eqs. (7), (13) and (21). Figure 17 shows the computed  $f_i$  from Eqs. (1) and (2) and Eqs. (7), (13) and (21).  $f_i$  increases with increasing  $D$  due to the increase in  $\delta$  shown in Fig. 16.  $J_G$  for a given  $J_G^*$  or  $K_G^*$  decreases with increasing  $P$  mainly due to the increase in  $\rho_G$ . There are no data to confirm validity of the calculated values, but they did not show unreasonable trends.

Eq. (23) for  $f_i$  gave irrationally small  $f_i$  for large  $D^*$  due to the term of  $D^{*-2.9}$  for the coefficient  $A$ . Eq. (22) for  $f_i$  gave small change of  $f_i$  for changing  $K_G^*$  due to the term of  $D^{*-0.50}$  for the exponent  $B$  in comparison with  $f_i$  calculated by Eqs. (1), (2), (7), (13) and (21).  $f_i = A \exp(B K_G^*)$  was better than  $f_i = A K_G^{*B}$  in Eq. (22), hence  $A$  and  $B$  for  $f_i = A \exp(B K_G^*)$  were obtained for  $f_i$  shown in Fig. 17 by using the least square method.  $A$  and  $B$  were expressed by functions of  $D^*$  and  $\rho_G/\rho_L$ . As a result, we derived the following  $f_i$  correlation.

$$f_i = A \exp(B K_G^*),$$

$$A = \left( \frac{3.76}{10^4} \right) \left( \frac{\rho_L}{\rho_G} \right)^{0.76} D^{*0.76},$$

$$B = -0.654 \left( \frac{\rho_L}{\rho_G} \right)^{0.11} D^{*0.16} \quad \text{for } 15 \leq D^* \leq 187. \quad (30)$$

Figure 18 shows  $f_{i,corr}$  calculated by Eq. (30) comparing with  $f_{i,cal}$  shown in Fig. 17.  $f_{i,corr}$  and  $f_{i,cal}$  agreed well for air-water conditions except small  $f_i$  ( $< 0.01$ ). Wallis<sup>1</sup> suggested  $f_i > 0.005$  and the  $f_i$  value in the region of  $f_i < 0.01$  is not important. The difference between  $f_{i,corr}$  and  $f_{i,cal}$  became large at high pressures. Eq. (22) or (23) agreed better for the  $f_i$  data with relatively small diameters than Eq. (30).

#### IV.C. Correlation for Drift-Flux Parameters

From Eqs. (24)-(26),  $\langle \alpha \rangle = \langle J_G \rangle / \{ \langle J_G + J_L \rangle + V_{gj} \}$ . Eq. (27) or (29) cannot be applied to large  $D$  and high  $P$  because of  $\alpha > 1.0$  due to  $\{ \langle J_G + J_L \rangle + V_{gj} \} < J_G$  for small  $J_G$

(i.e. large  $|J_L|$ ).  $\alpha$  can be obtained from Eq. (17) and  $\delta$  by Eq. (21). The correlation for the drift velocity  $V_{gj}$  was obtained from  $C_0 = 1$ ,  $\delta$  in Fig. 8 (a) by data, and Fig. 16 by Eq. (21) as:

$$V_{gj}^* = \max(A, B), 0 \leq V_{gj}^* \leq 2.2 \text{ for } 7.8 \leq D^* \leq 187$$

$$A = 1.0 \frac{(\rho_L / \rho_G)^{0.24}}{D^{*0.20}} - 0.315 \left( \frac{\rho_L}{\rho_G} \right)^{0.317} K_G^*,$$

$$B = 0.76 \frac{(\rho_L / \rho_G)^{0.15}}{D^{*0.20}} - 0.515 \left( \frac{\rho_L}{\rho_G} \right)^{0.032} \ln(K_G^*). \quad (31)$$

$V_{gj}^* = 0$  and  $2.2$  in  $0 \leq V_{gj}^* \leq 2.2$  show the lower and upper limits of  $V_{gj}^*$ , respectively. The first term  $A$  and second term  $B$  are for low  $P$  and high  $P$ , respectively. Figure 19 shows the relationship between  $\alpha_{corr}$  by Eqs. (24), (26) and (31) and  $\alpha_{cal}$  by Eq. (21) (i.e.  $\delta$  shown in Fig. 16).  $\alpha_{corr}$  was lower than  $\alpha_{cal}$  at low  $\alpha$  for medium  $D$ . Eq. (27) or (29) agreed better for the  $\alpha$  data with relatively small diameters than Eq. (31). It was difficult to derive a  $V_{gj}^*$  correlation for wide range of conditions, and it is recommended to obtain a  $V_{gj}^*$  correlation for a given  $D$ .

## V. CONCLUSIONS

In this study, we compared the data by Goda et al.<sup>6</sup> for  $D = 40$  mm with the rounded top and square bottom ends (R/S) and the data by Takaki et al.<sup>8</sup> for  $D = 40$  mm with the square top and rounded bottom ends (S/R) to evaluate features of flow characteristics for the rough film (RF) due to flooding at the bottom end and the smooth film (SF) due to flooding at the top end. We obtained the liquid film  $\delta$  (or void fraction  $\alpha$ ) and interfacial friction factor  $f_i$  by using the correlation of the wall friction factor  $f_w$  proposed by Takaki et al.<sup>8</sup> and  $dP/dz$  data reported by Bharathan et al.<sup>3</sup> and Ilyukhin et al.,<sup>9</sup> and we derived empirical correlations for  $\delta$  and  $f_i$  for SF.

- (1) For SF in the region of low  $J_G$ ,  $(1-\alpha)$  and  $f_i$  under flooding conditions were larger for R/S than they were for S/R due to large  $J_L$  for R/S.
- (2)  $\delta$  for SF was well expressed by a function of the liquid Reynolds number  $Re_L$  as  $\delta \propto Re_L^{1/3}$  (i.e. Nusselt equation),  $Re_L^{1/2}$  and  $Re_L^{2/3}$  for the laminar flow, transition, and turbulent flow, respectively. The uncertainty of the correlation proposed for  $\delta$ , Eq. (21), which included 95 % of the data points, was  $\pm 0.0062$  for  $\alpha = 0.87$ -0.98.
- (3)  $\delta/L$  (where  $L$  is Laplace length) was better than the gas Kutateladze parameter  $K_G^*$  to express  $f_i$  for SF, and Eq. (23) was derived as a function of  $\delta/L$ , the dimensionless diameter  $D^*$ , and the density ratio of gas and liquid phases  $\rho_G/\rho_L$ . On the other hand, Eq. (30) (which was a function of  $K_G^*$ ,  $D^*$ , and  $\rho_G/\rho_L$ ) was recommended for large  $D$  and high pressure  $P$ .
- (4) The drift-flux parameters ( $C_0$  and  $V_{gj}$ ) for SF were evaluated. The distribution parameter was  $C_0 = 1$  due to the annular flow, and a correlation for the dimensionless drift velocity  $V_{gj}^*$  was derived as a function of  $K_G^*$  and the viscosity ratio of gas and liquid phases  $\mu_G/\mu_L$ . The uncertainty (which included 95 % of the data points) was  $\pm 0.013$  for  $\alpha$  computed with the drift-flux Eqs. (24), (26) and (29), which could not be applied to large  $D$  and high  $P$ . Eq. (31) was proposed for  $V_{gj}^*$  at large  $D$  and high  $P$ .

## NOMENCLATURE

$C$	CCFL constant (-)
$C_0$	distribution parameter (-)
$D$	pipe diameter (m)
$D^*$	dimensionless pipe diameter (-)
$f_i$	interfacial friction factor (-)

$f_w$	wall friction factor (-)
$g$	gravitational acceleration (m/s <sup>2</sup> )
$h$	water level in the upper tank (m)
$J$	superficial velocity (m/s)
$J^*$	Wallis parameter (-)
$K^*$	Kutateladze parameter (-)
$L$	Laplace length (m)
$L_v$	length defined by Eq. (14) (m)
$m$	slope of CCFL characteristics (-)
$P$	pressure (Pa)
$Re$	Reynolds number (-)
$V_{gj}$	drift velocity (m/s)
$V_{gj}^*$	dimensionless drift velocity (-)
$W_L$	liquid flow rate limited by flooding (m <sup>3</sup> /s)
$z$	axial coordinate (m)

#### *Greek*

$\alpha$	void fraction (-)
$\delta$	liquid film thickness (m)
$\mu$	viscosity (Pa s)
$\nu$	kinematic viscosity (m <sup>2</sup> /s)
$\rho$	density (kg/m <sup>3</sup> )
$\sigma$	surface tension (N/m)

#### *Subscript*

$B$	bottom
$c$	computed

$G$	gas phase
$i$	$G$ or $L$
$L$	liquid phase
$m$	measured
$T$	top
<i>Superscript</i>	
*	dimensionless form

## References

1. G. B. WALLIS, *One-Dimensional Two-Phase Flow*, pp. 336-345, McGraw Hill, New York (1969).
2. S. G. BANKOFF, and S. C. LEE, "A Critical Review of the Flooding Literature," NUREG/CR-3060, U.S. Nuclear Regulatory Commission (1983).
3. D. BHARATHAN, G. B. WALLIS, and H. J. RICHTER, "Air-Water Countercurrent Annular Flow in Vertical Tubes," EPRI NP-786, Electric Power Research Institute (1978).
4. D. BHARATHAN, G. B. WALLIS, and H. J. RICHTER, "Air-Water Countercurrent Annular Flow," EPRI NP-1165, Electric Power Research Institute (1979).
5. D. BHARATHAN, and G. B. WALLIS, "Air-Water Countercurrent Annular Flow," *Int. J. Multiphase Flow*, **9**, 4, 349 (1983); [https://doi.org/10.1016/0301-9322\(83\)90093-9](https://doi.org/10.1016/0301-9322(83)90093-9).
6. R. GODA et al., "Experimental Study on Interfacial and Wall Friction Factors under Counter-Current Flow Limitation in Vertical Pipes with Sharp-Edged Lower Ends," *Nucl. Eng. Des.*, **353**, 110223 (2019); <https://doi.org/10.1016/j.nucengdes.2019.110223>.

7. T. SHIMAMURA et al., “Interfacial and Wall Frictions under Flooding Conditions in a Vertical Pipe with the Sharp-Edged Upper End,” *Proc. of Jpn. Symposium on Multiphase Flow 2018*, Sendai, Japan, August 8-10, 2018, D212 (in Japanese).
8. T. TAKAKI et al., “Flow Characteristics in Vertical Circular Pipes with the Square Top End under Flooding Conditions,” *Nucl. Eng. Des.*, **371**, 110951 (2021); <https://doi.org/10.1016/j.nucengdes.2020.110951>.
9. Yu. N. ILYUKHIN et al., “Hydrodynamic Characteristics of Annular Counter Flows in Vertical Channels,” *Teplofiz. Vys. Temp.*, **26**, 5, 923 (1988) (in Russian).
10. T. DOI et al., “Countercurrent Flow Limitation at the Junction Between the Surge Line and the Pressurizer of a PWR,” *Sci. Technol. Nucl. Installations*, **2012**, 754724 (2012); <https://doi.org/10.1155/2012/754724>.
11. M. MURASE et al., “Effects of Diameters on Countercurrent Flow Limitation at a Square Top End in Vertical Pipes,” *Sci. Technol. Nucl. Installations*, **2018**, 1426718, (2018); <https://doi.org/10.1155/2018/1426718>.
12. T. TAKAKI et al., “Liquid Film Thickness in Vertical Circular Pipes under Flooding Conditions at the Top End,” *Nucl. Technol.*, **206**, 3, 389 (2020); <https://doi.org/10.1080/00295450.2019.1656521>.
13. N. ZUBER, and J. FINDLAY, “Average Volumetric Concentration in Two-Phase Flow Systems,” *J. Heat Transfer*, **87**, 453 (1965).
14. T. KUSUNOKI et al., “Effects of Fluid Properties on CCFL Characteristics at a Vertical Pipe Lower End,” *J. Nucl. Sci. Technol.*, **52**, 887 (2015); <https://doi.org/10.1080/00223131.2014.990533>.
15. T. KUSUNOKI et al., “Condensation Experiments for Counter-Current Flow Limitation in an Inverted U-Tube,” *J. Nucl. Sci. Technol.*, **53**, 486 (2016); <https://doi.org/10.1080/00223131.2015.1057253>.



16. Y. SUDO, "Limitation of Falling Water in Countercurrent Two-Phase Flow in Vertical Circular Tubes," *Trans. of the JSME*, **60**, 2566 (1994) (in Japanese); <https://doi.org/10.1299/kikaib.60.2566>.
17. N. SANO et al., "Interfacial Friction Factors in Vertical Circular Pipes under Flooding Conditions at the Bottom End," *Jpn. J. Multiphase Flow*, **34**, 82 (2020) (in Japanese); <https://doi.org/10.3811/jjmf.2020.029>.
18. S. KAMEI et al., "Hold-Up in a Wetted Wall Tower," *Kagaku-kogaku*, **18**, 545 (1954) (in Japanese).
19. K. FEIND, "Strömungsuntersuchungen bei Gegenstrom von Rieselfilmen und Gas in Lotrechten Rohren," *VDI-Forschungsheft*, **481** (1960) (in German).
20. G. F. HEWITT, and G. B. WALLIS, "Flooding and Associated Phenomena in Falling Film Flow in a Tube," AERE-R4022, Atomic Energy Research Establishment (1963).
21. W. NUSSELT, "Die Oberflächenkondensation des Wasserdampfes," *Vereines Deutscher Ingenieure*, **60**, 541 (1916) (in German).
22. H. IMURA et al., "Flooding Velocity in a Counter-Current Annular Two-Phase Flow," *Chemical Eng. Sci.*, **32**, 79 (1977); [https://doi.org/10.1016/0009-2509\(77\)80199-1](https://doi.org/10.1016/0009-2509(77)80199-1).
23. W. BRÖTZ, "Über die Vorausberechnung der Absorptionsgeschwindigkeit von Gasen in Strömenden Flüssigkeitsschichten," *Chemie. Ing. Techn.*, **26**, 470 (1954) (in German).
24. H. BRAUER, "Strömungsuntersuchungen und Wärmeübergang bei Rieselfilmen," B22, VDI Forschungsheft, 457 (1956) (in German).
25. G. B. WALLIS, and S. MAKKENCHERY, "The Hanging Film Phenomenon in Vertical Annular Two-Phase Flow," *J. Fluids Eng.* **96**, 3, 297 (1974); <https://doi.org/10.1115/1.3447155>.

26. G. B. WALIS, and J. T. KUO, "The Behavior of Gas-Liquid Interfaces in Vertical Tubes," *Int. J. Multiphase Flow*, **2**, 521 (1976); [https://doi.org/10.1016/0301-9322\(76\)90013-6](https://doi.org/10.1016/0301-9322(76)90013-6).

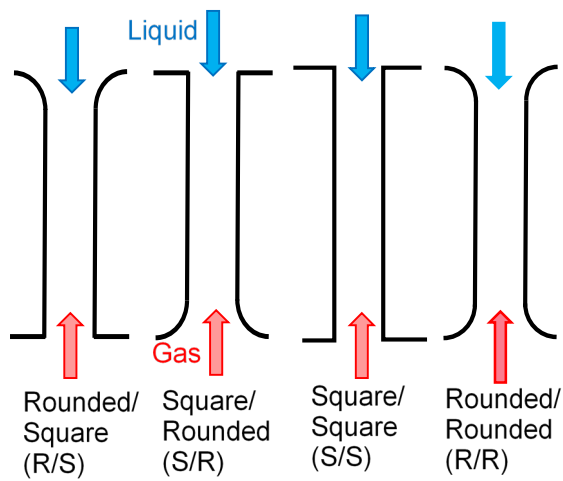
TABLE I

Experimental Conditions

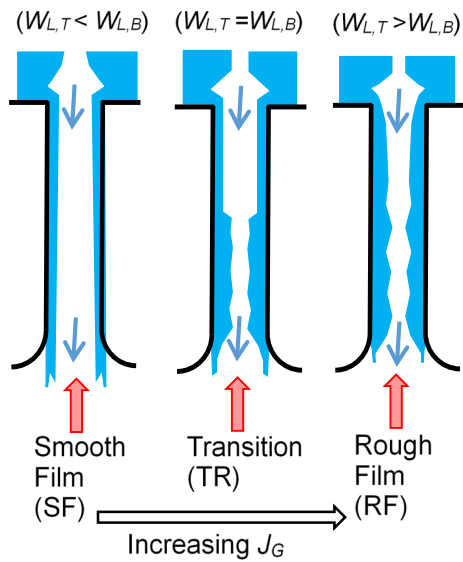
Reference	$D$ (mm)	Top/Bottom	Fluids	$P$ (MPa)	$h$ (m)	Data
Goda et al. <sup>6</sup>	20, 40	R/S	A-W	0.1	0.1	$\alpha$ , $dP/dz$
Shimamura et al. <sup>7</sup>	20	S/R	A-W	0.1	0.1	$\alpha$ , $dP/dz$
Takaki et al. <sup>8</sup>	40	S/R	A-W	0.1	0.1	$\alpha$ , $dP/dz$
Bharathan et al. <sup>3</sup>	50.8	S/S, S/R, R/S	A-W	0.1	> 0.1	$\delta$ , $dP/dz$
Ilyukhin et al. <sup>9</sup>	20	S/S	S-W	0.6-4.1	(high)	$dP/dz$

Top/Bottom: R, rounded; S, square. Fluids: A, air; S, steam; W, water.

$D$ , diameter;  $h$ , water level in the upper tank;  $P$ , pressure;  $dP/dz$ , pressure gradient;  
 $\alpha$ , void fraction;  $\delta$ , liquid film thickness



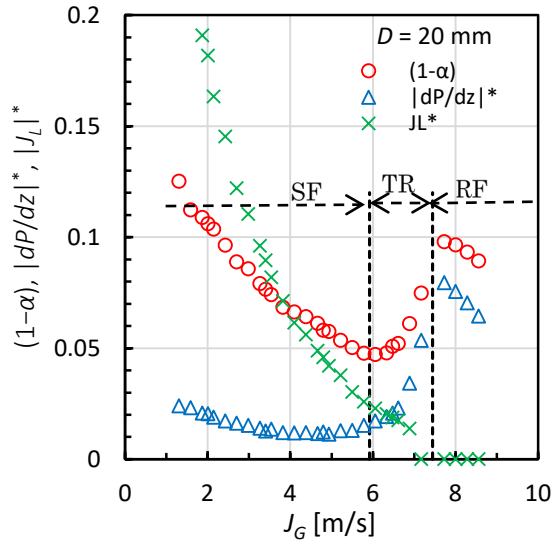
(a) Top and bottom end shapes



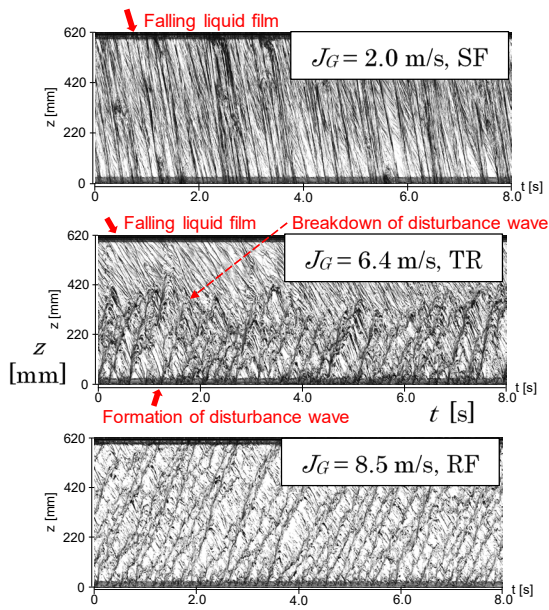
(b) Flow patterns under flooding conditions

( $W_L$ , liquid flow rate limited by flooding;  $B$ , bottom end;  $T$ , top end)

Fig. 1. Illustrations for top and bottom end shapes and flow patterns.



(a) Flow characteristics



(b) Time-strip images

Fig. 2. Features of flow characteristics and flow patterns in a vertical pipe with the square top and rounded bottom ends under flooding conditions reported by Shimamura et al.<sup>7</sup> (SF, smooth film; TR, transition; RF, rough film).

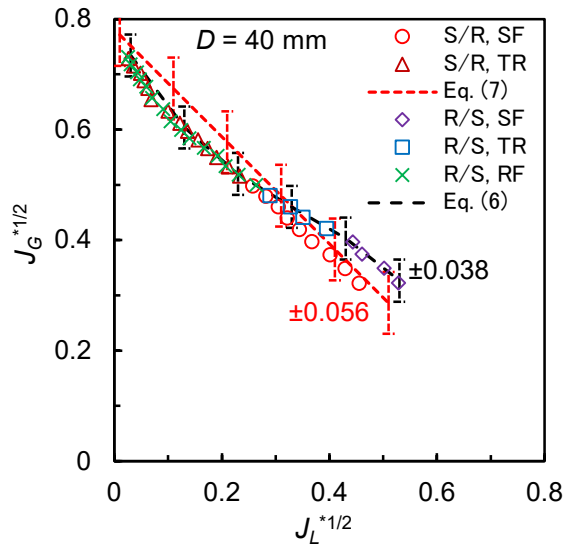


Fig. 3. CCFL characteristics (S/R and R/S, see Table I; SF, smooth film; TR, transition, RF, rough film).

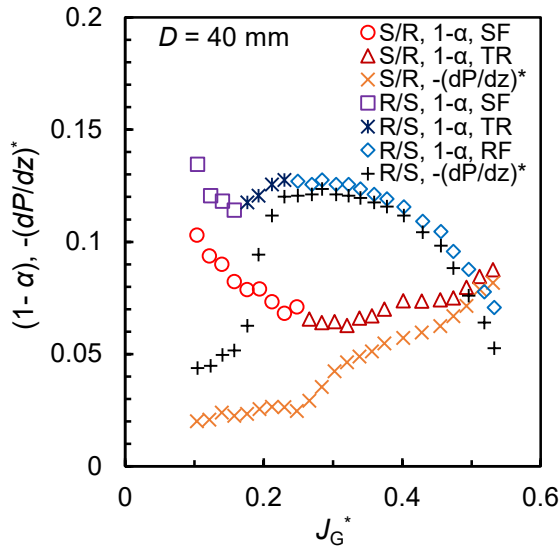


Fig. 4. Liquid volume fraction  $(1-\alpha)$  and dimensionless pressure gradient  $(dP/dz)^*$ .

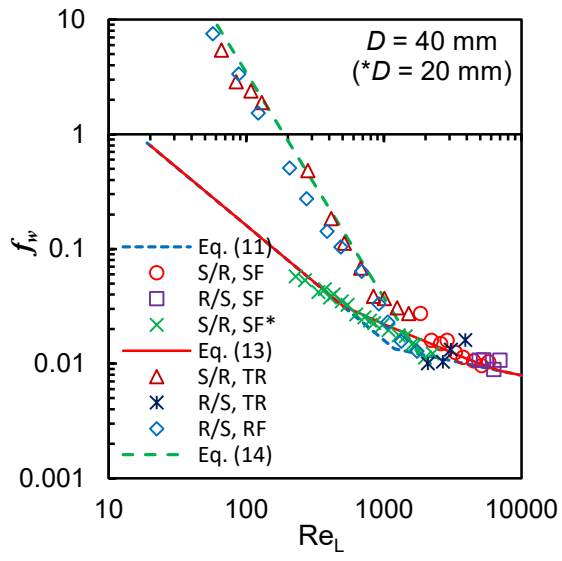


Fig. 5. Wall friction factor  $f_w$  (\*Shimamura et al.<sup>7</sup>).

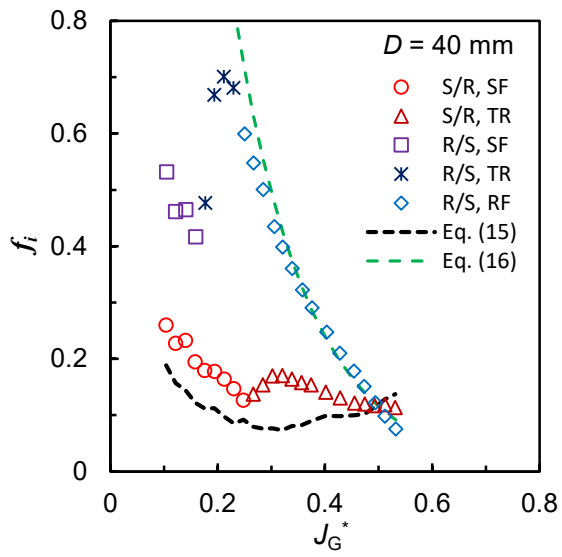


Fig. 6. Interfacial friction factor  $f_i$ .

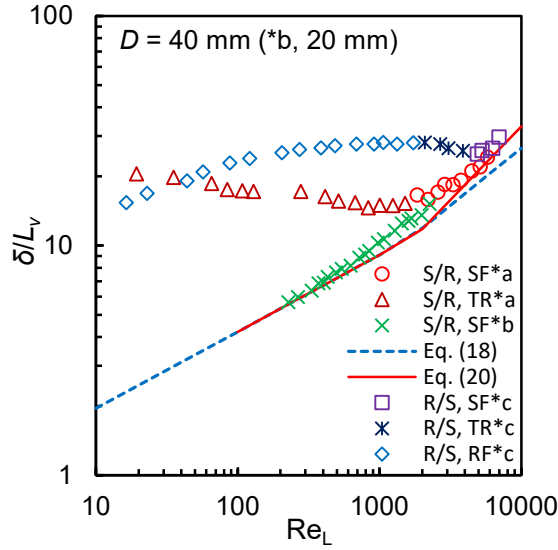


Fig. 7. Dimensionless liquid film thickness  $\delta/L_v$  (\*a, Takaki et al.<sup>8</sup>; \*b, Shimamura et al.<sup>7</sup>, \*c, Goda et al.<sup>6</sup>).

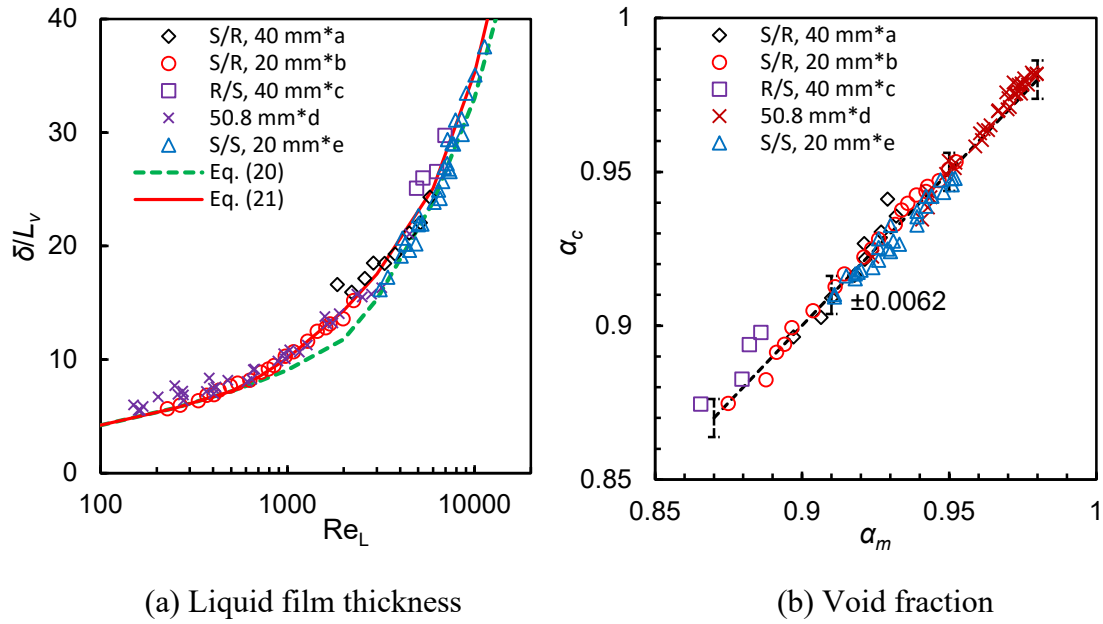


Fig. 8. Comparison of Eq. (21) with data for the liquid film thickness  $\delta/L_v$  and void fraction  $\alpha$ .  $\alpha_c$  and  $\alpha_m$  are  $\alpha$  computed with Eq. (21) and  $\alpha$  measured, respectively (\*a, Takaki et al.<sup>8</sup>; \*b, Shimamura et al.<sup>7</sup>; \*c, Goda et al.<sup>6</sup>; \*d, Bharathan et al.<sup>3</sup>; \*e, Ilyukhin et al.<sup>9</sup>).



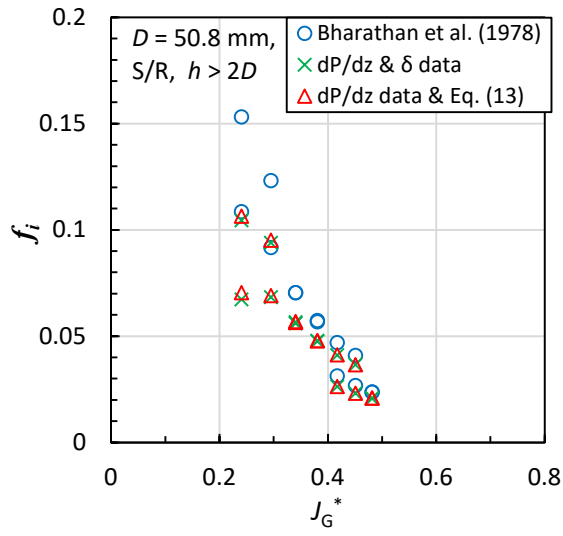


Fig. 9. Interfacial friction factor  $f_i$  obtained from data by Bharathan et al.<sup>3</sup>

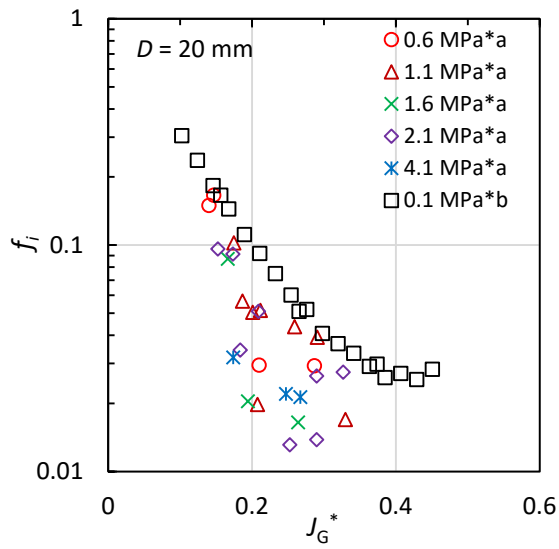
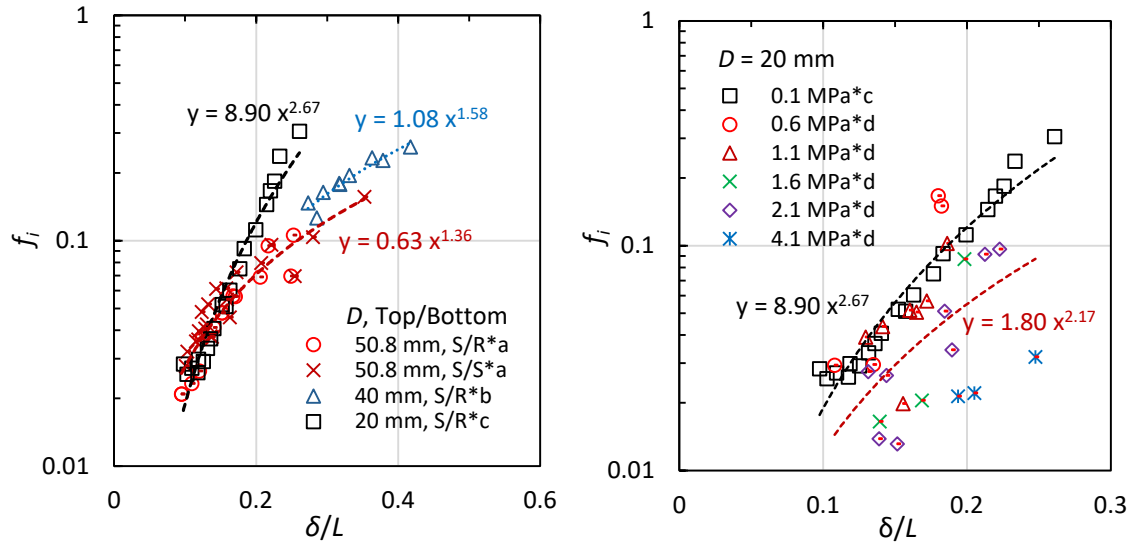
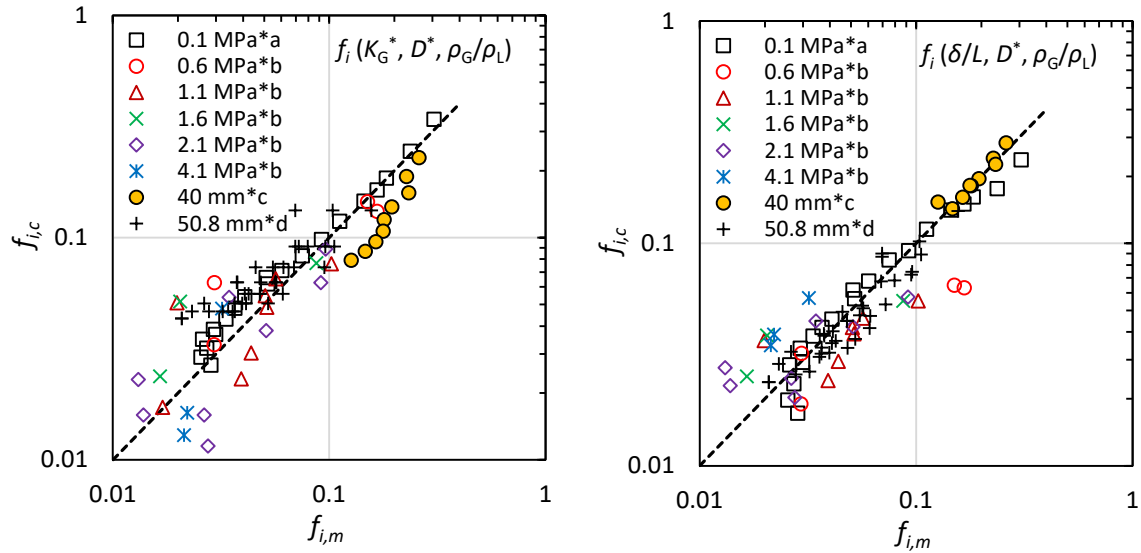


Fig. 10. Interfacial friction factor  $f_i$  obtained from data reported by Ilyukhin et al.<sup>9</sup> (\*a, Ilyukhin et al.<sup>9</sup>; \*b, Shimamura et al.<sup>7</sup>).



(a) Effects of diameters with air-water (b) Effects of fluid properties with  $D = 20$  mm

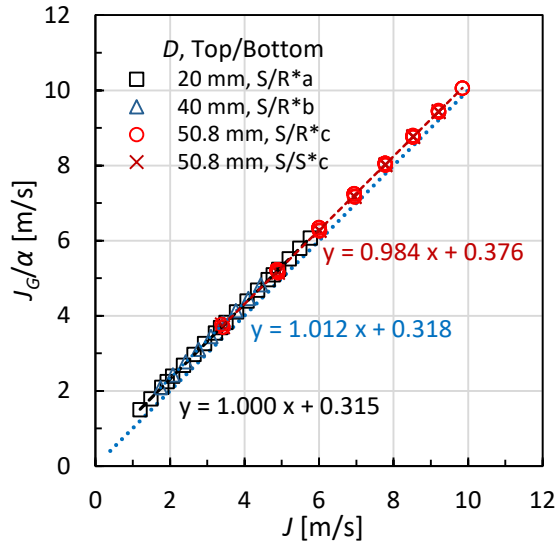
Fig. 11. Effects of diameters and fluid properties on  $f_i$  as a function of  $\delta/L$  (\*a, Bharathan et al.<sup>3</sup>; \*b, Takaki et al.<sup>8</sup>; \*c, Shimamura et al.<sup>7</sup>; \*d, Ilyukhin et al.<sup>9</sup>; S/R and S/S, see Table I;  $x = \delta/L$ ;  $y = f_i$ ).



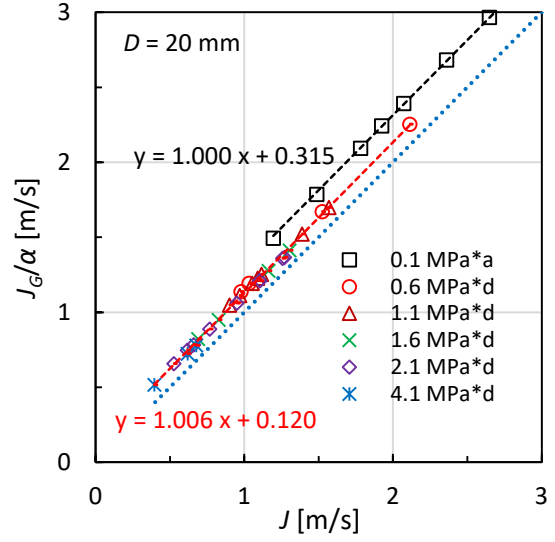
(a)  $f_{i,c}$  computed with Eq. (22)

(b)  $f_{i,c}$  computed with Eq. (23)

Fig. 12. Comparison of  $f_{i,c}$  values computed with the derived correlations, Eqs. (22) and (23), with the measured  $f_{i,m}$  (\*a, Shimamura et al.<sup>7</sup>; \*b, Ilyukhin et al.<sup>9</sup>; \*c, Takaki et al.<sup>8</sup>; \*d, Bharathan et al.<sup>3</sup>; \*a and \*b,  $D = 20$  mm).

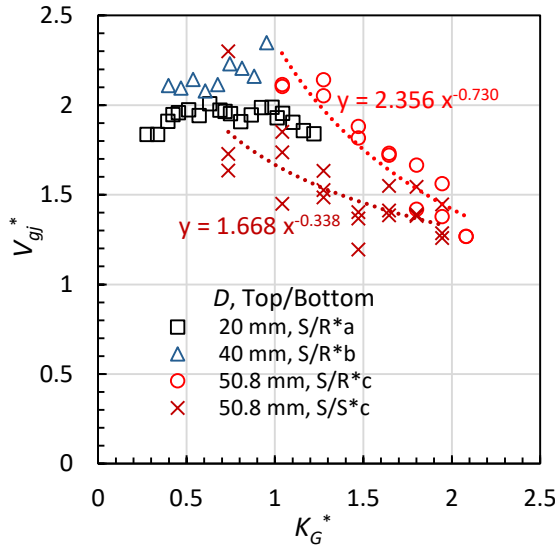


(a) Air-water conditions

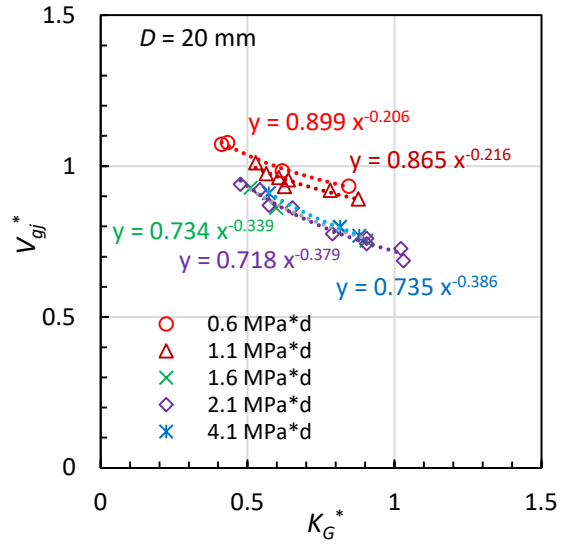


(b)  $D = 20$  mm (effects of fluid properties)

Fig. 13. Drift-flux plots for the SF (\*a, Shimamura et al.<sup>7</sup>; \*b, Takaki et al.<sup>8</sup>; \*c, Bharathan et al.<sup>3</sup>; \*d, Ilyukhin et al.<sup>9</sup>;  $x = J$ ;  $y = J_G/\alpha$ ).

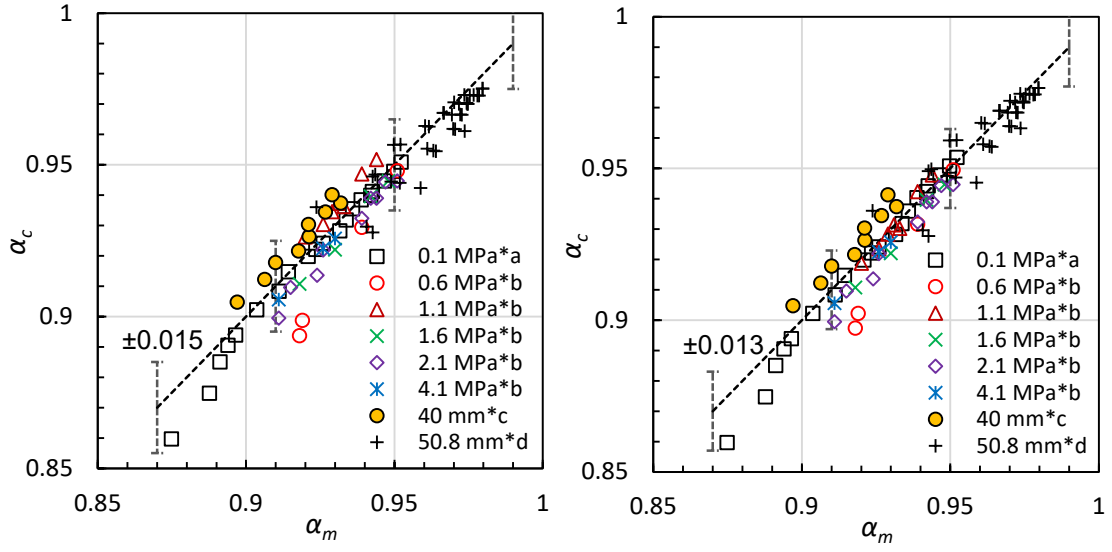


(a) Air-water conditions



(b) Steam-water conditions ( $D = 20$  mm)

Fig. 14. Dimensionless drift velocity  $V_{gj}^*$  with approximation of  $C_0 = 1$  (\*a, Shimamura et al.<sup>7</sup>; \*b, Takaki et al.<sup>8</sup>; \*c, Bharathan et al.<sup>3</sup>; \*d, Ilyukhin et al.<sup>9</sup>;  $x = K_G^*$ ;  $y = V_{gj}^*$ ).

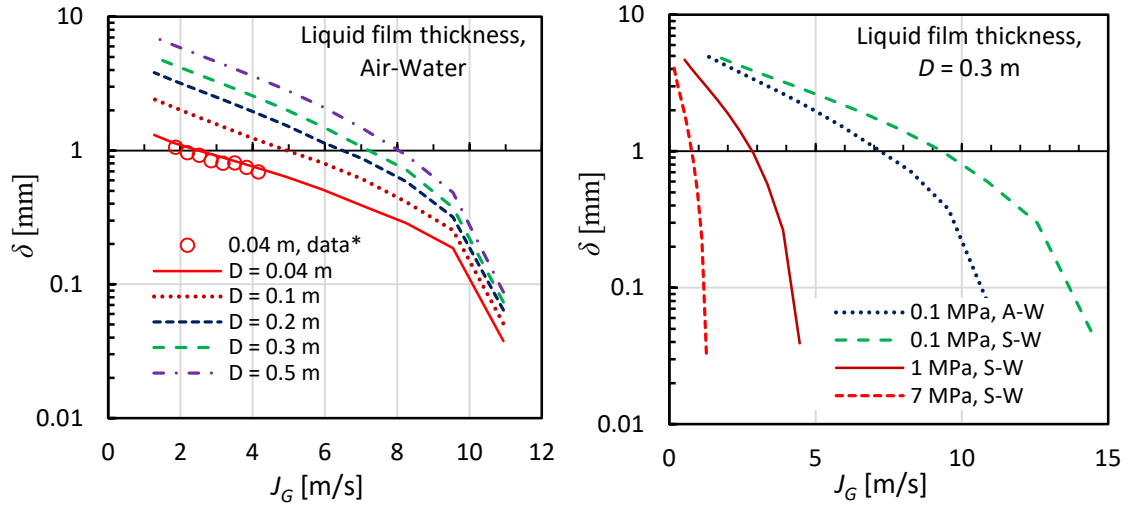


(a) Eqs. (24), (26) and (27)

(b) Eqs. (24), (26) and (29)

Fig. 15. Comparison of  $\alpha_c$  computed with the drift-flux correlation with the measured  $\alpha_m$

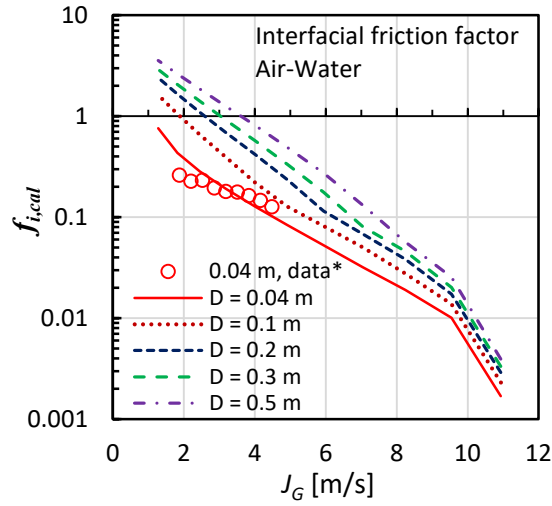
(\*a, Shimamura et al.<sup>7</sup>; \*b, Ilyukhin et al.<sup>9</sup>; \*c, Takaki et al.<sup>8</sup>; \*d, Bharathan et al.<sup>3</sup>).



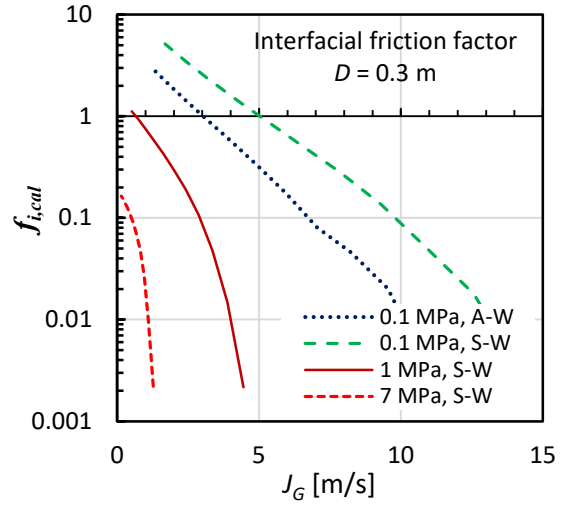
(a) Effects of diameters (air-water)

(b) Effects of pressures (S-W: steam-water)

Fig. 16. Liquid film thickness calculated by Eq. (21) (\*Takaki et al.<sup>8</sup>).

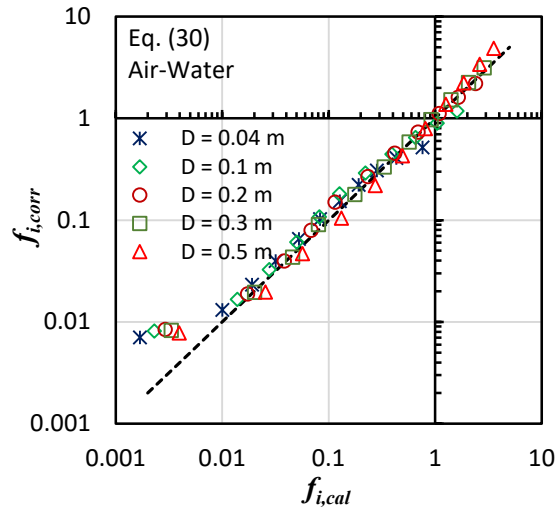


(a) Effects of diameters (air-water)

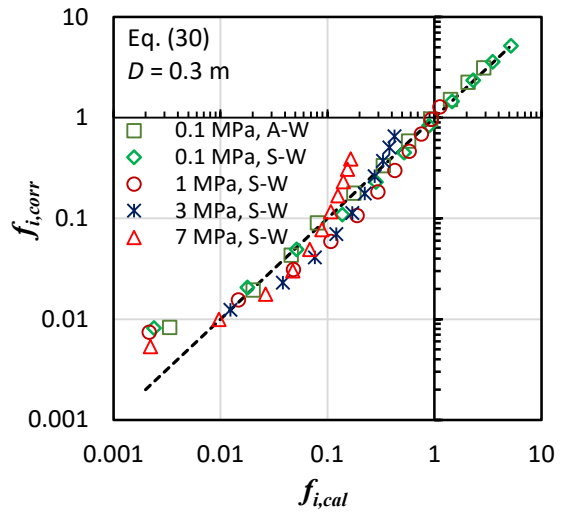


(b) Effects of pressures (S-W: steam-water)

Fig. 17. Interfacial friction factor  $f_{i,cal}$  calculated from Eqs. (1) and (2) and Eqs. (7), (13) and (21) (\*Takaki et al.<sup>8</sup>).

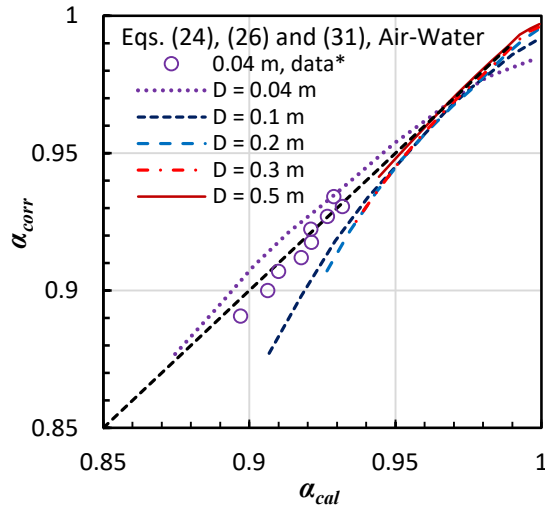


(a) Effects of diameters (air-water)

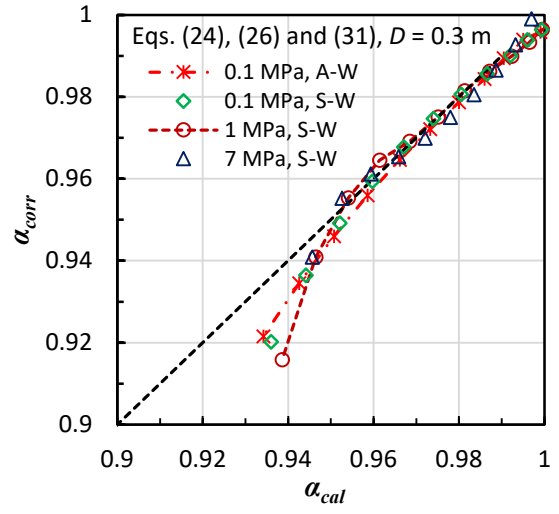


(b) Effects of pressures (S-W: steam-water)

Fig. 18. Interfacial friction factor  $f_{i,corr}$  calculated by the correlation of Eq. (30) for large  $D$  and high  $P$ .



(a) Effects of diameters (air-water)



(b) Effects of pressures (S-W: steam-water)

Fig. 19. Relationship between  $\alpha_{corr}$  by Eqs. (24), (26) and (31) and  $\alpha_{cal}$  by Eq. (21)

(\*Takaki et al.<sup>8</sup>).