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# MHz-Driven Snubberless Soft-Switching Current-Fed Multiresonant DC-DC Converter 

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#### Abstract

A new multiresonant step-up dc-dc converter is proposed in this article, which is suitable for obtaining a high dc-dc voltage ratio with minimizing the counts of active and passive components. The proposed dc-dc converter features the snubberless zero current soft-switching (ZCS) commutation with megahertz ( MHz ) high frequency driving of GalliumNitride-High Electron Mobility Transistor (GaN-HEMT)based two-phase class-E inverters by adopting quasi resonance and dual parallel load resonance; multiresonant circuitry. The circuit configuration and operation principle are described together with the theory of switch-mode transitions and steadystate power transfer. A frequency-domain analysis is provided on the basis of the equivalent circuit, and the design guideline of multiresonant tanks is provided in details. The essential performances of the proposed dc-dc converter are demonstrated by experiment of $1-2 \mathrm{MHz} / 120 \mathrm{~W}$ prototype; ZCS operations are confirmed over the wide range of load variations (40-100 \%) with maximum efficiency $91.3 \%$ at $86.5 \%$ load, electro magnetic interference (EMI) noise reduction $29-79 \%$ as compared to hard switching, and the voltage ratio 1.5 times higher than the nonmultiresonant topology, and less than $1 \%$ low-current ripple factor in the de inductor.


Index Terms-current-fed high frequency inverter, high stepup dc-dc converter, interleaved, multiresonant converter, snubberless, zero current soft-switching (ZCS).

## I. Introduction

AStep-up dc-dc converter is the essential power converter for renewable and sustainable power system, transportation electrifications, and a wide variety of circuit topologies have been proposed during the past decades. In particular, the high step-up ratio is one of the critical performance indexes in the dc-dc converters so that the energy utilization is enhanced while efficient power conversion can attain. Downsizing the converter scale is also a technically popular concern in the latest power electronics application, accordingly high-frequency switching, e.g. Megahertz ( MHz ) driving technique has great relevance with achievement of high power density[1]-[7]. The MHz -driven step-up dc-dc converter offers compact and lowprofile scale as well as high modularity, the suitable applications of which includes the emerging power electronics applications such as piezoelectric energy harvester, fuel cell, and class-E power amplifier of wireless power transfer (WPT)[8].
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The existing high step-up dc-dc converters are divided into: the stacked connection ([9][10]), switched capacitor / inductor ([11]-[13]), voltage multiplier ([14]), reconfigurable ([15][16]), edge resonant ([17][18]), and multi resonance ([19]). The overview of those existing topologies are summarized in TABLEI. Those step-up dc-dc converters exhibit high voltage ratio, however the counts of active and passive components inevitably increase and cost effectiveness may be lost. In contrast, current-fed dc-dc converters with high frequency link naturally attain voltage step-up by overlapping the ON-duty cycles of two active switches (over $50 \%$ ). In particular, the two-phase single-ended current-fed dc-dc converter is a good candidate for MHz-driven step-up dc-dc converters in terms of relatively simple circuit topology as well as the common ground gate drivers[20].
The high efficiency and low electromagnetic interference (EMI) noises switching performance plays a key role in the MHz-driven power converters while the related technologies include the developments of materials for magnetic components such as high frequency transformer (HF-X) and inductors, and PCB layouts with the reduced leakage inductances[3][21][22]. As a soft switching technique for MOS-gated controlled active power devices, zero voltage softswitching (ZVS) is suitable for treating the capacitive charges in the parasitic capacitances. However, the circulating current inherently is induced in the resonant networks, which leads to the complicated commutation process between the power devices with the aid of auxiliary circuit for the wide range of ZVS performance. In particular, the current-fed dc-dc converter as aforementioned cannot achieve the soft switching without any auxiliary active clamp circuit or active snubber [11]. The quasi-resonant ZVS current-fed dc-dc converters utilizing the leakage inductance of HF-X and the parasitic capacitances of power devices was also proposed in [18]. However, circulating current still exists in the high frequency inverter stage, thus MHz switching cannot be ensured in the type of current-fed dc-dc converter.

As a solution for the technical limitation and constraint of ZVS, a current-fed dc-dc converter featuring snubberless zero current soft-switching (ZCS) of GaN-HEMT with MHz switching was proposed as schematically drawn in Fig. 1[23]. This topology is based on the quasi-resonant and $L C$ resonant converters, and is free from the parasitic ringings of active switches which is inherent to the ZCS-pulse width modulation (PWM) dc-dc converters[24], owing to the voltageclamping effect on the parallel capacitor in the secondary-side of HF-X. Although the similar approach was proposed in the
past decade[25], the originality exists in the MHz driving by snubberless structure together with the dc coupled inductors for further reduction of passive components. The technical constraint of the previously-proposed topology in [23] is the voltage ratio inherently depends on the transformer turns ratio and voltage doubler rectifier. Thus, the technical challenge of the snubberless dc-dc converter is how to enhance the stepup ratio by decoupling the edge resonance and parallel load resonance.

In order to overcome the technical constraint on increasing the step-up ratio, a new multiresonant high step-up dcdc converter is proposed in this article. The multiresonant circuitry in the secondary-side of HF-X is dedicated for lifting the voltage without losing the merits of snubberless structure. Therefore, snubberless ZCS technique with multiresonant tank is attractive for the MHz-driven current-fed dc-dc converter in terms of soft switching range, counts of active and passive components, as well as reduction of reactive current. The novelty and originality exist in the multi-resonant topology; edge-resonant for ZCS, anti-resonant for reduction of magnetizing current in the HF-X, and parallel-load resonant for high step-up ratio, all of which are comprised by only the passive components under the conditions of MHz switching. It is suitable and beneficial for MHz-driven power converter in terms of practical and cost-effective circuit topology since no additional active switches are necessary together with the snubber components. In addition, the simplicity, high stepup voltage ratio, low current ripple in the dc input source together with the galvanic isolation are significantly advantageous for renewable power generation systems and energy harvest devices such as photovoltaic, liquid hydrogen / fuel cells and piezoelectric devices applied for the industry, distributed power, automotive, home and consumer electronics.

The article [23] was dedicated for the basic and original type of MHz driven snubberless ZCS dc-dc converter, where the operation principle and analysis on the PFM-based power regulations were described and followed by the experimental verification on the snubberless topology. It leads to the original idea of high step-up dc-dc converter with simple but practical circuit topology as treated herein. It is true the newly proposed dc-dc converter is modified and extended from the basic type by adding the parallel load resonant tank in the secondary side. However, the strategies on analysis and design of the main circuit have the different approaches from the basic type in terms of resonant converters, accordingly the descriptions and experimental results are different from [23].

The rest of this article is organized as follows: the circuit topology and operation principle of the proposed multiresonant dc-dc converter are described in Section II. The steadystate characteristics of dc-dc voltage ratio are revealed in the frequency-domain analysis, whereby the pulse-frequencymodulation (PFM)-based load voltage and power regulations are theoretically explained in Section III. In addition, the design guideline of circuit parameters is also presented in the same section so that the snubberless ZCS and high step-up voltage regulation attain simultaneously. The switching performances and steady-state characteristics on the load power and voltage ratio are investigated together with electromagnetic


Fig. 1. Snubberless ZCS step-up dc-dc converter[23].
noises by experiment in Section IV, after which the effectiveness of the proposed dc-dc converter is verified from the practical point of view in Section V.

## II. Circuit Topology and Operation Principle

The circuit topology of the proposed high step-up dc-dc converter is described with PFM-based power controller in Fig. 2.

The power stage of the primary-side HF-X consists of the current-fed two-phase class-E inverters which operate by the interleaved gate clocking in the active switches $\mathrm{Q}_{1}$ and $\mathrm{Q}_{2}$. Note here that any additional capacitive snubbers are not necessary in the two-phase class-E inverters. The secondaryside HF rectifier comprises of an antiparallel capacitor $C_{a}$ and the parallel-load resonant circuit $L_{p}-C_{p}$, the latter of which works for voltage lifting. The secondary-side rectifier of HFX is the voltage doubler, and other multiplier rectifiers can be candidates in accordance with the step-up ratio. The controller consists of voltage and current dual loops of the dc load. The pulse modulations is based on PFM and over $50 \%$ ONduty ratio in $\mathrm{Q}_{1}$ and $\mathrm{Q}_{2}$. The load voltage is detected and compared with its reference, after which their difference is processed by error amplifier (EA). The output of the voltage error amplifier (EA) is the command value to the load current, and the current loop with the another EA generates the control value. The control signal is processed by V/F converter, and ON-duty signal is generated by V/F converter. The pulse signal from the V/F converter is feed to a time delay circuit corresponding to the edge-resonant interval, then the gate signal of $S_{1}$ is produced through an OR logic circuit. The counterpart of gate signal $S_{2}$ is also generated by the same logic with $180^{\circ}$ of phase shift by a NOT gate.
The key operating waveforms of the main circuit and gate signals are depicted in Fig. 3. The ZCS commutations complete at the intervals of the two-switch overlapping "ON" states. The dc current ripples in $i_{L 1}$ and $i_{L 2}$ are ideally canceled out by the interleaved manner, so that the low ripple in the input side can maintain as low profile. The voltage $v_{C a}$ across $C_{a}$ is lifted by the effect of the anti-parallel load resonant tank $L_{p}-C_{p}$.

The mode transitions of switching one-cycle can be divided into eight modes as depicted in Fig. 4. The ideal conditions are given as: i) the inductance of $L_{1}$ and $L_{2}$ are identical as expressed by $L_{d}=L_{1}=L_{2}$, ii) the on-resistances of $\mathrm{Q}_{1}$ and $Q_{2}$ are small enough to neglect. The dc inductor currents

TABLE I
Comparison of High Step-Up Dc-Dc Converters

| Circuit topology | References | Numbers of power devices/ passive comp. | Switching frequency/ Pulse modulation | Input/output Voltages | Soft-switching Efficiency |
| :---: | :---: | :---: | :---: | :---: | :---: |
| stacked connection | [9] | 4/6 | $50 \mathrm{kHz} / \mathrm{PWM}$ | $20 \mathrm{~V} / 400 \mathrm{~V}$ | $\begin{aligned} & \hline \text { NR } \\ & 94 / 1 \% @ 320 \mathrm{~W} \end{aligned}$ |
|  | [10] | 7/5 | $50 \mathrm{kHz} / \mathrm{PWM}$ | $20 \mathrm{~V} / 402 \mathrm{~V}$ | $\begin{aligned} & \text { NR } \\ & 93.3 \% @ 250 \mathrm{~W} \end{aligned}$ |
| switched capacitor/inductor | [12] | 6/6 | $100 \mathrm{kHz} / \mathrm{PWM}$ | $30-40 \mathrm{~V} / 600 \mathrm{~V}$ | $\begin{aligned} & \text { ZVS } \\ & 97.0 \% @ 600 \text { W } \end{aligned}$ |
|  | [13] | 9/8 | $40 \mathrm{kHz} / \mathrm{PWM}$ | $30 \mathrm{~V} / 400 \mathrm{~V}$ | $\begin{aligned} & \text { NR } \\ & 94 \% @ 200 \mathrm{~W} \end{aligned}$ |
| voltage multiplier and stack | [15] | 6/6 | $50 \mathrm{kHz} / \mathrm{PWM}$ | $5-10 \mathrm{~V} / 50-100 \mathrm{~V}$ | $\begin{aligned} & \text { NR } \\ & 94 \% @ 400 \mathrm{~W} \end{aligned}$ |
| reconfigurable | [16] | $8 \leq$ | $\begin{aligned} & 62-54 \mathrm{kHz} \\ & \text { PFM } \end{aligned}$ | $24-54 \mathrm{~V} / 800 \mathrm{~V}$ | $\begin{aligned} & \hline \text { ZVS } \\ & 96.1 \% @ 600 \text { W } \end{aligned}$ |
| edge resonance | [18] | 4/6 | $50 \mathrm{kHz} / \mathrm{PWM}$ | $45 \mathrm{~V} / 380 \mathrm{~V}$ | $\begin{aligned} & \text { ZVS } \\ & 95.7 \% @ 400 \text { W } \end{aligned}$ |
| multi resonance | [19] | 4N/ $1+2 \mathrm{~N}$ <br> (N-stage) | $20 \mathrm{MHz} / \mathrm{ON} \& \mathrm{OFF}$ | $15.7-30 \mathrm{~V} / 60 \mathrm{~V}$ | $\begin{aligned} & \text { ZVS/ZCS } \\ & \leq 96.5 \% @ 200 \mathrm{~W} \end{aligned}$ |
| snubberless | [23] | 2/2 | $\begin{aligned} & 1-2 \mathrm{MHz} \\ & \text { PFM } \end{aligned}$ | $10 \mathrm{~V} / 85 \mathrm{~V}$ | $\begin{aligned} & \overline{\text { ZCS }} \\ & 86.1 \% @ 70 \mathrm{~W} \end{aligned}$ |

*Counted by a discrete power device. NR: not reported.


Fig. 2. Proposed multiresonant high step-up dc-dc converter with power controller.
$i_{L 1}, i_{L 2}$ can be expressed in each mode while the steady-state time-domain equations of the other variables are summarized in Appendix:
[Mode $1\left(t_{0} \leq t<t_{1}\right)$ : Power transfer mode] The active switch $\mathrm{S}_{1}$ keeps ON -state while $\mathrm{Q}_{2}$ is OFF in this interval. Then, the magnetic energy is stored in $L_{1}$ while it is released to the load. The dc inductor currents can be expressed by

$$
\begin{align*}
& i_{L 1}(t)=\frac{(1+k) V_{i n}-k a v_{c a}}{\left(1-k^{2}\right) L_{d}} \cdot\left(t-t_{0}\right)+i_{L 1}\left(t_{0}\right)  \tag{1}\\
& i_{L 2}(t)=\frac{(1+k) V_{i n}-a v_{c a}}{\left(1-k^{2}\right) L_{d}} \cdot\left(t-t_{0}\right)+i_{L 2}\left(t_{0}\right) \tag{2}
\end{align*}
$$

where $k$ is the coupling coefficient of the coupled dc inductors $L_{1}, L_{2}$ while $a\left(=w_{1} / w_{2}\right)$ denotes the windings turns ratio of the HF-X.
[Mode $2\left(t_{1} \leq t<t_{2}\right)$ : Edge resonant mode ( $\mathrm{Q}_{2}$ ZCS turnon)]
The active switch $\mathrm{S}_{2}$ is turned on at $t_{1}$, then the edge resonance begins by the leakage inductance $L_{r}$ and the parallel capaci-
tor $C_{a}$ in the secondary-side power stage. The polarity of the HF-X primary windings current $i_{p}$ naturally changes, and the capacitor voltage $v_{c a}$ increases gradually with the aid of $L_{r}-C_{p}$ edge resonance. The dc inductor currents are expressed by

$$
\begin{align*}
& i_{L 1}(t)=\frac{(1+k) V_{i n}}{\left(1-k^{2}\right) L_{d}} \cdot\left(t-t_{1}\right)+i_{L 1}\left(t_{1}\right)  \tag{3}\\
& i_{L 2}(t)=\frac{(1+k) V_{i n}}{\left(1-k^{2}\right) L_{d}} \cdot\left(t-t_{1}\right)+i_{L 2}\left(t_{1}\right) \tag{4}
\end{align*}
$$

The primary-side transformer winding current $i_{p}$ is expressed by

$$
\begin{align*}
& i_{p}(t)=\frac{a v_{c a}}{\zeta} \sin \left\{\omega_{q}\left(t-t_{1}\right)\right\}+i_{p}\left(t_{1}\right)  \tag{5}\\
& i_{p}\left(t_{1}\right)=\frac{i_{s}\left(t_{1}\right)}{a} \simeq 2 I_{o}  \tag{6}\\
& \zeta=a \sqrt{\frac{L_{r}}{C_{a}}}, \quad \omega_{q}=\frac{a}{2 \pi \sqrt{L_{r} C_{a}}} \tag{7}
\end{align*}
$$

[Mode 3 ( $t_{2} \leq t<t_{3}$ ): Edge-resonant mode ( $\mathrm{Q}_{1}$ ZCS turnoff)] The switch current $i_{\mathrm{Q}_{1}}$ naturally reaches to zero at $t_{2}$. By removing the gate-signal during this interval, ZCS turn-off can attain in $\mathrm{Q}_{1}$. The condition of ZCS commutation from $\mathrm{Q}_{2}$ to $Q_{1}$ is defined as

$$
\begin{equation*}
\zeta<\frac{v_{c a}}{2 I_{o}} \tag{8}
\end{equation*}
$$

[Mode $4\left(t_{3} \leq t<t_{4}\right)$ : Parallel-load resonant mode] The switch current $i_{\mathrm{Q} 2}$ is identical to the dc input current $i_{\text {in }}$ at $t=t_{3}$, whereby the edge resonance is terminated. The switch current $i_{L 2}$ increases linearly while $\mathrm{S}_{2}$ keeps ON -state.

$$
\begin{align*}
& i_{L 1}(t)=\frac{(1+k) V_{i n}-a v_{c a}}{\left(1-k^{2}\right) L_{d}} \cdot\left(t-t_{3}\right)+i_{L 1}\left(t_{3}\right)  \tag{9}\\
& i_{L 2}(t)=\frac{(1+k) V_{i n}-k a v_{c a}}{\left(1-k^{2}\right) L_{d}} \cdot\left(t-t_{3}\right)+i_{L 2}\left(t_{3}\right) \tag{10}
\end{align*}
$$



Fig. 3. Key voltage and current waveforms during the switching one cycle.
[Mode $5\left(t_{4} \leq t<t_{5}\right)$ : Power transfer mode] The voltage $v_{C p}$ across the parallel load-resonant capacitor $C_{p}$ exceeds to the voltage $V_{C_{o 1}}$ at $t=t_{4}$, and the rectifying diode $\mathrm{D}_{\mathrm{o} 1}$ is forward-biased.
[Mode 6 ( $t_{5} \leq t<t_{6}$ ): Edge-resonant mode ( $\mathrm{Q}_{1}$ ZCS turnon)] The switch $\mathrm{S}_{1}$ is turned on at $t=t_{5}$, then the edge resonance is resumed. The current $i_{\mathrm{Q} 1}$ increases gradually, and ZCS turn-on can attain in $\mathrm{Q}_{1}$. The dc inductor currents are expressed by

$$
\begin{align*}
i_{L 1}(t) & =\frac{(1+k) V_{i n}}{\left(1-k^{2}\right) L_{d}} \cdot\left(t-t_{5}\right)+i_{L 1}\left(t_{5}\right)  \tag{11}\\
i_{L 2}(t) & =\frac{(1+k) V_{i n}}{\left(1-k^{2}\right) L_{d}} \cdot\left(t-t_{5}\right)+i_{L 2}\left(t_{5}\right) \tag{12}
\end{align*}
$$


(a) Mode 1

(b) Mode 2

(c) Mode 3

(d) Mode 4

$$
\begin{align*}
& i_{p}(t)=\frac{a v_{c a}}{\zeta} \sin \left\{\omega_{r}\left(t-t_{5}\right)\right\}+i_{p}\left(t_{5}\right)  \tag{13}\\
& i_{p}\left(t_{5}\right)=\frac{i_{s}\left(t_{5}\right)}{a} \simeq 2 I_{o} \tag{14}
\end{align*}
$$

[Mode 7 ( $t_{6} \leq t<t_{7}$ ): Edge-resonant mode ( $\mathrm{Q}_{2}$ ZCS turnoff)] The switch current $i_{\mathrm{Q}_{2}}$ naturally reverses its direction at $t=t_{6}$, then the diode $\mathrm{D}_{2}$ of $\mathrm{Q}_{2}$ is conducting. During this interval, the gate signal to $\mathrm{S}_{2}$ is removed, then ZCS turn-off can attain in $\mathrm{Q}_{2}$.
[Mode 8 ( $t_{7} \leq t<t_{8}$ ): Parallel-load resonant] The switch current $i_{\mathrm{Q}_{1}}$ is equal to the input current $i_{i n}$ at $t=t_{7}$, whereby the edge resonance is terminated. The two dc inductor currents $i_{\mathrm{L}_{1}}$ and $i_{\mathrm{L}_{2}}$ flows into $\mathrm{Q}_{1}$; $i_{\mathrm{L}_{1}}$ linearly increases while $i_{L_{2}}$ gradually decreases.

$$
\begin{align*}
& i_{L 1}(t)=\frac{(1+k) V_{i n}-k a v_{c a}}{\left(1-k^{2}\right) L_{d}} \cdot\left(t-t_{7}\right)+i_{L 1}\left(t_{7}\right)  \tag{15}\\
& i_{L 2}(t)=\frac{(1+k) V_{i n}-a v_{c a}}{\left(1-k^{2}\right) L_{d}} \cdot\left(t-t_{7}\right)+i_{L 2}\left(t_{7}\right) \tag{16}
\end{align*}
$$



Fig. 4. Mode transitions and equivalent circuits during the switching one cycle.


Fig. 5. Simplified equivalent circuit with the primary-side referred parameters: $L_{m}^{\prime}=a^{2} L_{m}, L_{p}^{\prime}=a^{2} L_{p}, C_{a}^{\prime}=C_{a} / a^{2}, C_{p}^{\prime}=C_{p} / a^{2}$, and $R_{a c}^{\prime}=$ $a^{2} R_{a c}$.

## III. Steady-State Characteristics

## A. Frequency-Domain Analysis

The simplified equivalent circuit is depicted in Fig. 5. Assuming that the power losses in $C_{\mathrm{o} 1}$ and $C_{\mathrm{o} 2}$ are small
enough for neglecting, the sinusoidal approximation theory can be applied for the proposed topology. Thus, the ac equivalent resistance $R_{a c}$ can be expressed by

$$
\begin{equation*}
R_{a c}=\frac{2 V_{o}}{\pi^{2} I_{o}}=\frac{2}{\pi^{2}} R_{L} \tag{17}
\end{equation*}
$$

The impedance $Z_{i n}$ viewed from the input dc source $V_{i n}$ can be defined as [26]

$$
\begin{equation*}
\dot{Z}_{i n}=\dot{Z}_{i 0} \frac{1+\frac{R_{a c}^{\prime}}{\dot{Z}_{o 0}}}{1+\frac{R_{a c}^{\prime}}{\dot{Z}_{o \infty}}}=\dot{Z}_{i \infty} \frac{1+\frac{\dot{Z}_{o 0}}{R_{a c}^{\prime}}}{1+\frac{\dot{Z}_{o \infty}}{R_{a c}^{\prime}}} \tag{18}
\end{equation*}
$$

where each impedance can be expressed as

$$
\begin{equation*}
\dot{Z}_{i 0}=\frac{1}{j \omega C_{a}^{\prime}+\frac{L_{m}^{\prime}+L_{p}^{\prime}}{j \omega L_{m}^{\prime} L_{p}^{\prime}}}+j \omega L_{r} \tag{19}
\end{equation*}
$$

$$
\begin{align*}
& \dot{Z}_{i \infty}=\dot{Z}_{1}+j \omega L_{r}, \\
& \dot{Z}_{1}=\left\{j \omega C_{a}^{\prime}+\frac{1}{j \omega L_{m}^{\prime}}+\frac{1}{j \omega L_{p}^{\prime}+\frac{1}{j \omega C_{p}^{\prime}}}\right\}^{-1}  \tag{20}\\
& \dot{Z}_{o 0}=\frac{1}{j \omega C_{p}^{\prime}+\dot{Z}_{3}^{-1}}, \dot{Z}_{3}=j \omega L_{p}^{\prime}+\dot{Z}_{2}  \tag{21}\\
& \dot{Z}_{2}=\left\{\frac{L_{m}^{\prime}+L_{r}}{j \omega L_{m}^{\prime} L_{r}+j \omega C_{a}^{\prime}}\right\}^{-1} \tag{22}
\end{align*}
$$

$$
\dot{Z}_{o \infty}=\frac{1}{\frac{1}{\bar{Z}_{4}+j \omega L_{p}^{\prime}}+j \omega C_{p}^{\prime}}
$$

$$
\begin{equation*}
\dot{Z}_{4}=\left\{j \omega C_{a}^{\prime}+\frac{1}{j \omega L_{m}^{\prime}}\right\}^{-1} \tag{23}
\end{equation*}
$$

Accordingly, the ac voltage ratio $M_{a c}$ can be expressed as

$$
\begin{align*}
M_{a c} & =\left|\left(1-\frac{j \omega L_{r}}{\dot{Z}_{i n}}\right) \cdot\left(\frac{1}{j \omega L^{\prime}{ }_{p} \dot{Y}_{5}+1}\right)\right|  \tag{24}\\
\dot{Y}_{5} & =j \omega C^{\prime}{ }_{p}+{R^{\prime}}_{a c}^{\prime-1} . \tag{25}
\end{align*}
$$

The frequency characteristics of $Z_{i n}$ and $M_{a c}$ are drawn in Fig. 6 by referring to (18) and (24) with a set of numerical example. The operating area should be set as the capacitive load area where the switching frequency is less than the resonant frequency of maximum ac voltage gain in $M_{a c}$.

On the other hand, the dc voltage ratio $G\left(=V_{o} / V_{i n}\right)$ should be derived from the viewpoint of power balance between the input and output in Fig. 5. In order to simply the analysis on the high-order resonant tank, the two-phase class-E inverter voltage $v_{a b}$ is linearly expressed in Fig. 2. Note here that linearization follows to the method in [23].
The dc voltage ratio of $G$ both for the basic and multiresonant types can be defined by

$$
\begin{align*}
G & =\frac{\sqrt{2} a R_{L}}{\pi} \times \frac{2 \sqrt{2} V_{i n}}{\pi(0.5-\lambda)} \sqrt{\sum_{n=1,3,5 . .}^{\infty} \frac{\cos ^{2}(\lambda n \pi)}{n^{2} z_{n}^{2}}} \\
& =\frac{4 a R_{L}}{\pi^{2}(0.5-\lambda)} \sqrt{\sum_{n=1,3,5 . .}^{\infty} \frac{\cos ^{2}(\lambda n \pi)}{n^{2} z_{n}^{2}}} \tag{26}
\end{align*}
$$



Fig. 6. Frequency-domain characteristics of the driving-point impedance ( $Z_{i n}$ ) in the ac equivalent circuit ( $L_{r}=44 \mathrm{nH}, L_{m}=25.6 \mu \mathrm{H}$, $C_{\mathrm{a}}=2.2 \mathrm{nF}, L_{p}=2 \mu \mathrm{H}, C_{p}=1 \mathrm{nF}$, and $a=w_{1} / w_{2}=1 / 2$ ).


Fig. 7. Theoretical characteristics of the dc-dc voltage conversion ratios (normalized by the voltage ratio of the basic type at 1 MHz ).
where $\lambda$ is defined as

$$
\begin{equation*}
\lambda=\frac{4 \pi \sqrt{L_{r} C_{a}} \cdot f_{s}}{5 a} \tag{27}
\end{equation*}
$$

In addition, $Z_{n}$ in (26) denotes $Z_{n, b}$ in (28) for the basic type and $Z_{n, m r}$ in (29) for the multi-resonant type, respectively:

$$
\begin{equation*}
Z_{n, b}=\sqrt{R_{a c}^{2}\left(a^{2}+\frac{L_{r}}{L_{m}}-n^{2} \omega^{2} L_{r} C_{a}\right)^{2}+n^{2} \omega^{2} L_{r}^{2}} \tag{28}
\end{equation*}
$$

The dc-dc voltage ratios of the proposed topologies are compared in Fig. 7 between the basic and proposed topologies. It can be known from the comparison that higher voltage ratio can achieve in the proposed converter.

## B. Design of Parameters in Resonant Tank

The impedances $Z_{r a}, Z_{p p}$ of the edge resonant $L_{r}-C_{a}$ and parallel-load resonant $L_{p}-C_{p}$, and admittance $Y_{m a}$ of antiresonant $L_{m}-C_{a}$ are presented in Fig. 8. The resonant frequencies can be defined as

$$
\begin{equation*}
f_{a}=\frac{1}{2 \pi \sqrt{L_{m} C_{a}}}, f_{p}=\frac{1}{2 \pi \sqrt{L_{p} C_{p}}}, f_{q}=\frac{a}{2 \pi \sqrt{L_{r} C_{a}}} \tag{30}
\end{equation*}
$$

where the condition expressed by $f_{a}<f_{s}<f_{p}<f_{q}$ should be satisfied. Once the ratios between the two frequencies are defined as

$$
\begin{equation*}
\alpha=\frac{f_{p}}{f_{a}}, \quad \beta=\frac{f_{q}}{f_{p}} \tag{31}
\end{equation*}
$$

where the relationships between magnetizing $L_{m}$, the parallel capacitor $C_{a}$, and leakage inductance $L_{r}$ are expressed by

$$
\begin{align*}
C_{a} & =\frac{1}{\omega_{a}^{2} L_{m}}, \quad \omega_{a}=2 \pi f_{a}  \tag{32}\\
L_{r} & =\frac{1}{\omega_{q}^{2} C_{a}}, \quad \omega_{q}=2 \pi f_{q} \tag{33}
\end{align*}
$$

It can be understood from Fig. 6 that the frequency range between $f_{a}$ and $f_{q}$ is most suitable for obtaining the effects of anti- and parallel-load resonant while edge-resonant frequency should exist in the higher frequency area. Accordingly, the anti-resonant frequency $f_{a}$ should be set in the area smaller than 1 MHz for deciding the switching frequency between 1 and $2 \mathrm{MHz} ; Y_{m a}, Z_{p p}<Z_{r a}$. Thus, $\alpha$ and $\beta$ should be greater than 1 respectively. By adjusting $\alpha$ and $\beta$ until the ZCS condition (8) is satisfied, the parameters of $C_{a}$ and $L_{r}$ can be determined by (32) and (33). Thereby, $\alpha$ and $\beta(\alpha<\beta)$ are decided between 1 and 3 from the practical point of views for MHz driving.

Furthermore, when the quality factor $Q$ in the parallel load resonant tank is set as the practical value, e.g. $1<Q<10$, $L_{p}$ can be decided by

$$
\begin{equation*}
L_{p}=\frac{R_{a c}}{\omega_{p} Q}, \quad \omega_{p}=2 \pi f_{p} \tag{34}
\end{equation*}
$$

Thus, the capacitor $C_{p}$ can be obtained as

$$
\begin{equation*}
C_{p}=\frac{1}{\omega_{p}^{2} L_{p}} \tag{35}
\end{equation*}
$$

## C. Coupled DC Inductors

The ripple factors of the two dc inductors can be defined by referring to one of the modes where they gradually increase. Now, by giving the average inductors currents $I_{L}, I_{i n}$ respectively, the ripple factors can be defined as

$$
\begin{align*}
\gamma_{L} & =\frac{(1+k) V_{i n}-a v_{c a}}{\left(1-k^{2}\right) L_{d} I_{L} f_{s}}(1-D)  \tag{36}\\
\gamma_{i n} & =\frac{2 V_{i n}-a v_{c a}}{(1-k) L_{d} I_{i n} f_{s}}(1-D) \tag{37}
\end{align*}
$$

where $D\left(=t_{o n} / T_{s}\right)$ is the ON-duty cycle of $\mathrm{Q}_{1}$ and $\mathrm{Q}_{2}$. The curves of current ripples are illustrated in Fig. 9 according to (36) and (37) with a set of numerical example ( $V_{i n}=10 \mathrm{~V}$, $L_{d}=L_{1}=L_{2}=25 \mu \mathrm{H}, v_{c a}=2 V_{i n}$ ). It can be known that $\gamma_{L}$ is minimum at $k=0.6$ while $\gamma_{i n}$ increases gradually in accordance with the increase of $k$.

## IV. Experimental Evaluations

## A. Specification of Prototype

The performances of proposed dc-dc converter are evaluated by experiment of $1-2 \mathrm{MHz} / 120 \mathrm{~W}$ prototype with GaN-HEMT (GS61004B, $V_{D S}=100 \mathrm{~V}, I_{D S}=38 \mathrm{~A}$, $R_{D S, \text { on }}=16 \mathrm{~m} \Omega, C_{\mathrm{oss}}=110 \mathrm{pF}, Q_{\mathrm{g}}=3.3 \mathrm{nC}, \mathrm{GaN}$

$$
\begin{align*}
& Z_{n, m r}=\frac{L_{m}}{L_{r}} \cdot \sqrt{\alpha^{2}+\beta^{2}} \\
& \alpha=R_{a c}\left\{1+\frac{a^{2} L_{m}}{L_{r}}+\left(\frac{n \omega}{\omega_{a}} \cdot \frac{n \omega}{\omega_{p}}\right)^{2}-\left(\frac{n \omega}{\omega_{a}}\right)^{2}-\left\{1+\frac{L_{m}\left(L_{r}+a^{2} L_{p}\right)}{L_{r} L_{p}}\right\}\left(\frac{n \omega}{\omega_{p}}\right)^{2}\right\} \\
& \beta=n \omega L_{p}\left\{1+\frac{L_{m}\left(L_{r}+a^{2} L_{p}\right)}{L_{r} L_{p}}-\left(\frac{n \omega}{\omega_{a}}\right)^{2}\right\} \tag{29}
\end{align*}
$$



Fig. 8. Impedances of the edge-resonant $L_{r}-C_{a}$, the load-resonant $L_{p}-C_{p}$, and admittance of the anti-resonant tank $L_{m}-C_{a}\left(L_{r}=44 \mathrm{nH}, L_{m}=\right.$ $25.6 \mu \mathrm{H}, C_{\mathrm{a}}=2.2 \mathrm{nF}, L_{p}=2 \mu \mathrm{H}, C_{p}=1 \mathrm{nF}$, and $\left.a=w_{1} / w_{2}=1 / 2\right)$.


Fig. 9. Current ripple ratios versus magnetically coupling coefficient in the dc side.

Systems) for $\mathrm{Q}_{1}, \mathrm{Q}_{2}$, and Silicon Carbide Schottky diode (SiCSBD) (IDH06G65C6, $650 \mathrm{~V}, 6 \mathrm{~A}$, typical $V_{F}: 1.25 \mathrm{~V}$, Infenion) for $\mathrm{D}_{\mathrm{o} 1}, \mathrm{D}_{\mathrm{o} 2}$, respectively. The exterior appearance of prototype is portrayed in Fig. 10. The circuit parameters and specification are displayed in TABLE II. Selection of 1.8 MHz for the rated power can be justified in line with the technical trend of automotive applications; $1.8 \mathrm{MHz}-2.2 \mathrm{MHz}$ is preferably selected in order to mitigate electro-magnetic interference from the dc-dc power converters.
The planar transformer is designed for $1-2 \mathrm{MHz}$ switching, and its core material is MnZn ferrite (PC200, ER-23/5/13). The magnetic core selection is based on a maximum magnetic flux density. The gate resistors of $\mathrm{Q}_{1}$ and $\mathrm{Q}_{2}$ are decided as $10 \Omega$ for minimizing parasitic ringings in MHz driving. The quality factor $Q$ of $L_{p}-C_{p}$ resonant tank in (34) is given as 2 at the


Fig. 10. Exterior appearances of prototype.

TABLE II
Circuit Parameters of Prototype

| Item | Symbol | Value |
| :---: | :---: | :---: |
| DC input voltage | $V_{\mathrm{in}}$ | 10 V |
| DC output voltage | $V_{\mathrm{o}}$ | $85-160 \mathrm{~V}$ |
| Output power rating | $P_{\mathrm{o}}$ | 120 W |
| Nominal Switching frequency | $f_{\mathrm{s}}$ | 1.8 MHz |
| Anti-resonant frequency | $f_{a}$ | 680 kHz |
| Load resonant frequency | $f_{p}$ | 3.8 MHz |
| Edge-resonant frequency | $f_{q}$ | 8.1 MHz |
| Duty cycle | $D$ | 0.56 |
| Input dc inductor | $L_{1}$ | $71 \mu \mathrm{H}$ |
| Input dc inductor | $L_{2}$ | $73 \mu \mathrm{H}$ |
| $L_{1}, L_{2}$ windings turns ratio | $n\left(=N_{1} / N_{2}\right)$ | 1 |
| Mutual inductance | $M$ | $43 \mu \mathrm{H}$ |
| Coupling coefficient | $k$ | 0.59 |
| HF-X magnetizing inductance | $L_{m}$ | $26 \mu \mathrm{H}$ |
| HF-X leakage inductance | $L_{r}$ | 45 nH |
| HF-X windings turns ratio | $a\left(=w_{1} / w_{2}\right)$ | $1 / 2$ |
| Anti-resonant capacitor | $C_{\mathrm{a}}$ | 2.2 nF |
| Load-resonant capacitor | $C_{\mathrm{p}}$ | 1 nF |
| Load-resonant inductor | $L_{\mathrm{p}}$ | $1.8 \mu \mathrm{H}$ |
| Voltage dividing capacitors | $C_{\mathrm{o} 1,2}$ | 180 nF |

nominal $R_{L}=200 \Omega$.

## B. Switching Performances and Steady-State Characteristics

The switching waveforms of the prototype can be observed in Fig. 11 for $f_{s}=1.1 \mathrm{MHz}$ (light load) and 1.5 MHz (heavy load) respectively. It can be observed in each cases that the current $i_{Q_{1}}$ gradually declines by edge resonant while the current $i_{\mathrm{Q}_{2}}$ gradually increases, which leads to ZCS turn-on in $\mathrm{Q}_{2}$ and ZCS turn-off in $\mathrm{Q}_{1}$ respectively. After the power


Fig. 11. Observed switching waveforms of active switches at: (a) $f_{s}=1.1 \mathrm{MHz}$ and $P_{o}=51 \mathrm{~W}\left(i_{\mathrm{Q} 1}, i_{\mathrm{Q} 2}: 2.5 \mathrm{~A} /\right.$ div, $v_{\mathrm{Q} 1}$, $v_{\mathrm{Q} 2}: 6 \mathrm{~V} / \operatorname{div}, v_{a b}: 10 \mathrm{~V} / \operatorname{div}, 200 \mu \mathrm{~s} / \mathrm{div}$ ), and (b) $f_{s}=1.5 \mathrm{MHz}$ and $P_{o}=104, \mathrm{~W}\left(i_{\mathrm{Q} 1}, i_{\mathrm{Q} 2}: 2.5 \mathrm{~A} / \operatorname{div}, v_{\mathrm{Q} 1}, v_{\mathrm{Q} 2}: 6 \mathrm{~V} / \mathrm{div}, v_{a b}: 10 \mathrm{~V} / \mathrm{div}\right.$, $200 \mu \mathrm{~s} / \mathrm{div})$.
transfer interval, $i_{\mathrm{Q}_{1}}$ starts to increase with a certain slope from zero by supplying the gate signal to $\mathrm{S}_{1}$ while $i_{\mathrm{Q}_{2}}$ declines gradually, which leads to ZCS turn-on in $\mathrm{Q}_{1}$ and ZCS turnoff in $\mathrm{Q}_{2}$ respectively. Thus, the feasibility of snubberless ZCS topology is verified for the light and heavy load conditions.

The resonant capacitor voltages $v_{C_{a}}$ and $v_{C_{p}}$ are also observed in Fig. 12. The amplitude of the parallel-resonant capacitor $v_{C_{p}}$ are lifted from that of $v_{C_{a}}$ at both the light and heavy loads, and the double voltage appears in the output voltage $V_{o}$ with the effect of the voltage doubler rectifier. Thus, step-up operations of the multi-resonant tank are demonstrated hereby.

The dc input current $I_{i n}$ is shown in Fig. 13. The ripple current is less than $0.1 \%$ for the average dc current $12 \mathrm{~A}: \gamma_{i n}$ is $0.83 \%$ while the theoretical value is calculated as $0.63 \%$ at $v_{c a}=56 \mathrm{~V}$ from (37). Thus, the effectiveness of (37) is verified herein.
The radiated noise emissions are measured by comparing with hard switching conditions in Fig. 14. The radiated noise is reduced by $29 \%$ from $11.4 \mu \mathrm{~W}$ to $8.1 \mu \mathrm{~W}$ at $f_{s}=1.5 \mathrm{MHz}$ due to the snubberless ZCS. Furthermore, it is reduced by $79 \%$ from $134.8 \mu \mathrm{~W}$ to $27.8 \mu \mathrm{~W}$ at $f_{s}=18 \mathrm{MHz}$. Thus, the effectiveness of snubberless ZCS is proven in the experimental result.
The steady-state characteristics of input-output dc voltage ratio $G$ are measured under the open loop control in Fig. 15. More than sixteen of $G$ can attain in the proposed topology, and 1.5 times higher than the previously proposed topology in Fig. 1. The maximum voltage ratio is 16 at $f_{s}=2 \mathrm{MHz}$.


Fig. 12. Observed capacitor waveforms at: (a) $f_{s}=1.1 \mathrm{MHz}$ and (b) $f_{s}=$ $1.5 \mathrm{MHz}\left(v_{\mathrm{Q} 2}: 15 \mathrm{~V} / \operatorname{div}, v_{a b}: 15 \mathrm{~V} / \operatorname{div}, V_{o}: 20 \mathrm{~V} / \operatorname{div}, 200 \mu \mathrm{~s} / \mathrm{div}\right)$.


Fig. 13. Observed waveform of the dc input current $I_{\text {in }}(2 \mathrm{~A} / \mathrm{div}$, and $200 \mu \mathrm{~s} /$ div).

Therefore, the higher voltage step-up can achieve in Fig. 15.
The steady-state characteristics of output power versus switching frequency are measured under the condition of $V_{o}=120 \mathrm{~V}$ in Fig. 16. It can be confirmed from the curve that $P_{o}$ increase gradually from 51 W with $f_{s}=1.1 \mathrm{MHz}$ up to about 120 W at $f_{s}=1.8 \mathrm{MHz}$. The complete ZCS operation can be obtained in the switching frequency 1 MHz to 1.8 MHz . Thus, the effectiveness of PFM-based power regulation with the snubberless ZCS is revealed in the curves.

## C. Power Conversion Efficiency and Loss Analysis

The actual efficiency of the prototype is presented in Fig. 17. The ZCS turn-on and -off operations can maintain up to $86.5 \%$ $\operatorname{load}\left(P_{o} \simeq 104 \mathrm{~W}, f_{s}=1.5 \mathrm{MHz}\right.$ ) while ZCS turn-off cannot attain from $86.5 \%$ to $100 \%$ load since (8) cannot be satisfied. The maximum efficiency is recorded as $91.3 \%$ at $86.5 \%$ load, and over $90 \%$ efficiency can be ensured in the load ratio of $70 \%-92 \%$.


Fig. 14. Observed spectrum of radiated noises (probing by Electro-Metrics EM-6992)


Fig. 15. Comparison of step-up dc-dc voltage ratio (open-loop condition).


Fig. 16. Output power versus switching frequency curves at $V_{o}=120 \mathrm{~V}$.

The power loss breakdown relevant to Fig. 17 is revealed in Fig. 18. The conduction losses of active switches and copper


Fig. 17. Actual efficiency curves for load variations.


Fig. 18. Power loss breakdown at $f_{s}=1.5 \mathrm{MHz}, P_{o}=104 \mathrm{~W}$ and $\eta=$ $91.3 \%$.
losses of HF-X account for a large part of the total loss. The iron loss is less than $1.2 \%$ in the total loss, thus is included in the "Other losses". The conduction losses in the secondary side are relatively high as compared to the primary side due to the multiresonant tanks. The power loss in the gate resistor is calculated with the gate charge $\mathrm{Q}_{\mathrm{g}}=3.3 \mathrm{nC}$, the gate driving voltage $\mathrm{V}_{\mathrm{DR}}=6 \mathrm{~V}$ at $f_{s}=1.5 \mathrm{MHz}$ as

$$
\begin{equation*}
P_{D}=\mathrm{Q}_{\mathrm{g}} \times V_{D R} \times f_{s}=30 \mathrm{~mW} \tag{38}
\end{equation*}
$$

, which accounts for about $0.3 \%$ in the total power loss.
The thermography image of the prototype in ten minutes after the start-up is shown in Fig. 19. The temperatures of $\mathrm{Q}_{1}$ and $\mathrm{Q}_{2}$ are measured as $43.2^{\circ} \mathrm{C}$ and $35.6^{\circ} \mathrm{C}$, respectively. The dc inductor, parallel resonant inductor, HF-X, and diode rectifiers have temperatures as $25.4^{\circ} \mathrm{C}, 43.5^{\circ} \mathrm{C}, 32.7^{\circ} \mathrm{C}$, and $38.6^{\circ} \mathrm{C}$, respectively. It should be remarked here that $\mathrm{Q}_{1}$ has higher temperature than $\mathrm{Q}_{2}$ due to the shorter distance from the HF-X.
The comparisons with the existing topologies are summarized in TABLE III in terms of modulation, voltage conditions, efficiency, and power density. It can be understood hereby that the proposed topology has competitive efficiency and power density as a high step-up MHz-driven dc-dc converter while almost all the existing topologies are limited to buck type which are prone to have higher efficiency due to less conduction losses in active switches.

TABLE III
Comparison of MHz-driven Dc-Dc converters

| Circuit topology | Galvanic isolation | Switching frequency | Modulations | Input/output Voltages | Soft-switching Peak Efficiency Power device | Power density |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Two-phase half-bridge[27] | isolated | 1 MHz | PWM | $\begin{aligned} & 36 \mathrm{~V}-60 \mathrm{~V} / 1.8 \mathrm{~V} \\ & \text { (buck) } \end{aligned}$ | ZVS\&ZVS NR@90 W GaN-HEMT (EPC2014) | - |
| Current-fed active-clamped[28] | isolated | 1 MHz | PWM | $\begin{aligned} & 25 \mathrm{~V} / 100 \mathrm{~V} \\ & \text { (boost) } \end{aligned}$ | ZVS | - |
| DC-X[29] | isolated | $1 \mathrm{MHz} / 300 \mathrm{kHz}$ | PWM | $\begin{aligned} & 48 \mathrm{~V} / 12 \mathrm{~V} \\ & \text { (buck) } \end{aligned}$ | ZVS/ZCS $95.2 \% @ 300 \mathrm{~W}$ Si-MOSFET (BSC098N10NS5) | $370 \mathrm{~W} / \mathrm{in}^{3}$ |
| LLC[30] | isolated | $\begin{aligned} & 1.2-2.5 \mathrm{MHz} \\ & / 300 \mathrm{kHz} \end{aligned}$ | PWM | $\begin{aligned} & 48 \mathrm{~V} / 12 \mathrm{~V} \\ & \text { (buck) } \end{aligned}$ | $\begin{aligned} & \text { ZVS } \\ & 94.5 \% @ 700 \text { W } \\ & \text { GaN-HEMT } \end{aligned}$ | $49 \mathrm{~W} / \mathrm{in}^{3}$ |
| Class-E2[31] | non-isolated | 20 MHz | ON/OFF | $\begin{aligned} & 9-18 \mathrm{~V} / 5 \mathrm{~V} \\ & \text { (buck) } \end{aligned}$ | $\begin{aligned} & \text { ZVS } \\ & 75 \% @ 10 \text { W } \\ & \text { GaN-HEMT } \\ & \text { (EPC2016) } \\ & \hline \end{aligned}$ | - |
| Active clamped[32] | isolated | 2 MHz | PWM | $\begin{aligned} & 18 \mathrm{~V} / 5 \mathrm{~V} \\ & \text { (buck) } \end{aligned}$ | $\begin{aligned} & \text { ZVS } \\ & 93.5 \% @ 25 \text { W } \\ & \text { Si-MOSFET } \\ & \text { (BSC097N06NS) } \end{aligned}$ | - |
| Two-phase buck[33] | non-isolated | 1 MHz | PFM | $\begin{aligned} & 12 \mathrm{~V} / 4 \mathrm{~V} \\ & \text { (buck) } \end{aligned}$ | $\begin{aligned} & \text { ZVS } \\ & 97.5 \% @ 24 \mathrm{~W} \\ & \text { GaN-HEMT } \\ & \text { (EPC2015C) } \\ & \hline \end{aligned}$ | - |
| LLC/parallel[34] | isolated | 1 MHz | PFM | $\begin{aligned} & 12 \mathrm{~V} / 5 \mathrm{~V} \\ & \text { (buck) } \end{aligned}$ | ZVS <br> 94\%@240W <br> GaN-HEMT <br> (EPC2020) | $53 \mathrm{~W} / \mathrm{in}^{3}$ |
| Flying Capacitor[35] | Non-isolated | 1 MHz | PFM | $\begin{aligned} & 400 \mathrm{~V} / 178 \mathrm{~V} \\ & \text { (buck) } \end{aligned}$ | ZVS <br> 94\%@200 W <br> GaN-HEMT <br> (GS66508B) | - |
| MHz driving snubberless[23] | isolated | $1-2 \mathrm{MHz}$ | PFM | $\begin{aligned} & 10 \mathrm{~V} / 85 \mathrm{~V} \\ & \text { (boost) } \end{aligned}$ | ZCS $86.1 \% @ 70 \mathrm{~W}$ GaN-HEMT (PGA26E19BA) | $17 \mathrm{~W} / \mathrm{in}^{3}$ |
| Proposed converter | isolated | $1-2 \mathrm{MHz}$ | PFM | $\begin{aligned} & 10 \mathrm{~V} / 160 \mathrm{~V} \\ & \text { (boost) } \end{aligned}$ | ZCS <br> $91.3 \% @ 104$ W <br> GaN-HEMT <br> (GS61004B) | $39 \mathrm{~W} / \mathrm{in}^{3}$ |

*Counted by a discrete power device.


Fig. 19. Thermography image of prototype in ten minutes after the start up at $24.5^{\circ} \mathrm{C}$ of the room temperature.

## V. Conclusions

A MHz-driving snubberless ZCS high step-up dc-dc converter with multiresonant circuitry has been proposed in this article. The multiresonant tank works for high step-up ratio without loosing the simplicity in the snubberless circuit topology and the low ripple in the input stage of dc-dc power converter. The frequency-domain analysis has been revealed the design guideline of the circuit parameters of the anti- and parallel load resonant circuits, then selection guideline of the coupling coefficient of the dc inductors has been theoretically provided by the steady-state characteristics for the input and dc inductor currents. In order to demonstrate the performances of the proposed dc-dc converter, the $1-2 \mathrm{MHz} / 120 \mathrm{~W}$ prototype has been built, and the snubberless ZCS operations under MHz driving and low ripple rations less than $1 \%$ have been verified by experiments as well as steady-state characteristics.

It has also been proven that the EMI noises are well reduced

TABLE IV
Steady-State Equations in Each Mode for the Half Cycle

| Intervals | Primary-side $L$-C network |
| :---: | :---: |
| Mode 1: $t \in\left[0, t_{1}\right]$ | $\begin{gathered} \hline \hline V_{L 1}-V_{L 2}+a L p \frac{d}{d t} i_{L p}(t)-L r \frac{d}{d t} i_{L 2}(t)+\frac{a V o}{2}=0 \\ v_{C a}(t)=L_{p} \frac{d i_{L p}}{d t}(t)+\frac{V_{o}}{2}=L_{m} \frac{d i_{L m}}{d t} \\ C_{a} \frac{d V_{C a}}{d t}(t)+i_{L m}(t)+i_{L p}(t)=-a i_{L 2}(t) \\ V_{L 1}=V_{i n} \\ V_{L 1}=L \frac{d}{d \neq} i_{L 1}(t)-M \frac{d}{d \neq} i_{L 2}(t) \\ V_{L 2}=L \frac{d}{d t} i_{L 2}(t)-M \frac{d}{d t} i_{L 1}(t) \\ \hline \end{gathered}$ |
| Mode 2 and 3: $t \in\left[t_{1}, t_{3}\right]$ | $\begin{gathered} i_{L 1}(t)=i_{L 1}\left(t_{1}\right)+\frac{V i n\left(t-t_{1}\right)(k+1)}{L\left(1-k^{2}\right)} \\ i_{L 2}(t)=i_{L 2}\left(t_{1}\right)+\frac{V_{i n}\left(t-t_{1}\right)(k+1)}{L\left(1-k^{2}\right)} \\ a L_{p} \frac{d i_{L p}}{d t}(t)-L_{r}\left(-\frac{d i_{Q 2}}{d t}(t)+\frac{V i n(k+1)}{L\left(1-k^{2}\right)}\right)+\frac{a V_{o}}{2}=0 \\ v_{C a}(t)=L_{p} \frac{d i_{L p}}{d t}(t)+\frac{V_{o}}{2}=L_{m} \frac{d i_{L m}(t)}{d t} \\ C_{a} \frac{d v_{C a}(t)}{d t}+i_{L m}(t)+i_{L p}(t)=-a\left(I_{L 2}\left(t_{1}\right)+\frac{V i n\left(t-t_{1}\right)(k+1)}{L\left(1-k^{2}\right)}\right)+a i_{Q 2}(t) \\ I_{L 1}\left(t_{1}\right)+I_{L 2}\left(t_{1}\right)+\frac{2 V_{i n}\left(t-t_{1}\right)(k+1)}{L\left(1-k^{2}\right)}=i_{Q 1}(t)+i_{Q 2}(t) \end{gathered}$ |
| Mode 4: $t \in\left[t_{3}, t_{4}\right]$ | $\begin{gathered} V_{L 1}-V_{L 2}+L r \frac{d i_{L 1}(t)}{d t}+a V_{C a}(t)=0 \\ V_{C a}(t)=L_{p} \frac{d i_{L p}(t)}{d t}+\frac{1}{C p} \int_{t_{7}}^{t} i_{L p}(\tau) d t=L_{m} \frac{d i_{L m}(t)}{d t} \\ C_{a} \frac{d V_{C a}(t)}{d t}+i_{L m}(t)+i_{L p}(t)=a i_{L 1}(t) \\ V_{L 2}=V_{i n} \end{gathered}$ |

( $29 \%-79 \%$ ) owing to the soft switching techniques as compared to the hard switching from the spectrums of radiation noises. The dc-dc voltage ratio increases more than 1.5 times as the existing snubberless dc-dc converter, thus high step-up operation has been clarified. The actual efficiency is recorded as $91.3 \%$ at $86.5 \%$ load while the power dissipation of magnetic components should be reduced for further efficiency improvement under the conditions of MHz driving.
The future researches include enhancement of power rating and power conversion efficiency by optimizing the design of magnetic components suitable for MHz driving. Furthermore, the validity of the closed loop controller will be demonstrated by experiments for steady-state and dynamics operations.

## Appendix

The steady-state equations of each modes are summarized in TABLE IV. Note here that the steady-state equations for the other half cycle operations (Mode 5-8) are symmetrical to those in TABLE IV. The voltage and current waveforms at each mode can be derived by giving the initial values at the mode 1 , and solving the high-order equations with the aid of computer calculations.

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