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## EFG at Sb site of filled Skutterudites

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#### Abstract

The electronic field gradients are obtained based on electronic bandstructure calculations for filled skutterudites. The LDA+U calculations have revealed that asymmetry parameters are affected from the anisotropic charge density distribution at the rare earth site for  $PrRu_4Sb_{12}$  and  $PrOs_4Sb_{12}$ , suggesting Sb atoms move in low temperatures.

Key words: electronic field gradients, bandstructure calculations, filled skutterudites PACS: 71.15.Mb; 71.20.Eh; 76.60.Gv

Filled skutterudites  $RT_4X_{12}$  (R=rare earths; T=Fe, Ru, Os; X=P, As, Sb) are well known because of the variety of the interesting physical properties [1]. Such properties are thought to be related to the unique electronic bandstructure [2] and the crystalline electronic field in the rare-earth site [3], which is surrounded by 12 pnictogens. Among them, PrOs<sub>4</sub>Sb<sub>12</sub> is well known as an unusual superconductor with a singlet ground state [4], PrRu<sub>4</sub>Sb<sub>12</sub> is, however, a typical s-wave superconductor also with a singlet ground state [5]. It has been revealed that with decreasing temperature the NQR frequency  $(\nu_Q)$  for  $\text{PrOs}_4\text{Sb}_{12}$  and  $\text{PrRu}_4\text{Sb}_{12}$ starts to increase around the temperature corresponding to the energy for the first excited level; 10 K and 70 K, respectively. This implies that anisotropic  $4f^2$ charge distribution affects the electronic field gradients (EFG) at Sb-site. To study the effect from the 4f electrons, EFG are calculated for a several filled skutterudite compounds. EFG can be calculated by using an FLAPW method [6–8]. Moreover, the charge distribution of the singlet  $4f^2$  ground state could be taken into account by using the LDA+U method [9].

Filled skutterudites crystallize in a unique bcc structure of a space group  $\text{Im}\bar{3}$   $(T_h^5, \#204)$ , where 12 pnictogens, at 24g site such as (0, u, v), form a cage of an icosahedron. The lattice parameters used in calculations are listed in Table 1. The EFG at Sb site are

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obtained based on an FLAPW bandstructure calculation, proposed by Blaha et al. [6]. To get well converged values, about 1,300 LAPWs and 195 sampling k points in the irreducible BZ (3,456 points in the BZ) are used for all calculations. For Sb at (0, u, v), the bc-plane is a mirror plane, so  $V_{ab}$  and  $V_{ca}$  in EFG tensor are zero, but  $V_{bc}$  is nonzero. (Here, we use a, b and c for the crystalographic axes.) One of the principle axes (the z-axis) is parallel to the a axis, and the others are on the bc-plane. After transforming the principle axes, EFG are obtained as  $V_{zz}$  and asymmetric parameter  $\eta = (V_{xx} - V_{yy})/V_{zz}$ , as listed in Table 1.

 $\nu_Q$  is proportinal to  $3/(2I(2I-1))QV_{zz}$ , where I stands for nuclear spin and Q for nuclear quadupole moment. To convert  $V_{zz}$  to  $\nu_Q$ , we use the Q values for Sb, as in the caption in Table 1, which are determined to reproduce the experimental  $\nu_Q$ . As seen in Table 1, the Q values for  $^{121}{\rm Sb}$  and  $^{123}{\rm Sb}$  could obtain good agreement with the experimental  $\nu_Q$  not only for similar  $V_{zz}$  values of skutterudites, but also for USb<sub>2</sub>. Therefore, these Q values seem to b quite reliable. Note that  $\eta$  does not depend on the values I and Q.

To involve the effect from the anisotropic charge distribution of  $4f^2$  singlet in Pr, we use the LDA+U method for PrRu<sub>4</sub>Sb<sub>12</sub> and PrOs<sub>4</sub>Sb<sub>12</sub> [1,10,11]. The LDA+U method used here has the generalized form for the system in which the spin-orbit interaction is involved and U is set as 0.4Ry [9]. For PrOs<sub>4</sub>Sb<sub>12</sub>, three other method are used; i)  $4f^2$  electrons are treated

Table 1 The lattice constants a, the internal lattice parameters u and v, the calculated EFG and  $\nu_Q$  ( $^{121}\nu_Q$  for  $^{121}$ Sb and  $^{123}\nu_Q$  for  $^{123}$ Sb) and asymmetry parameters  $\eta$  The lattice parameters for skutterudites are obtained in room temperature by K. Oikawa [12]. Nuclear quadrupole moments  $Q = -0.59 \times 10^{-28} m^2$  for  $^{121}$ Sb (I=5/2) and  $Q = -0.75 \times 10^{-28} m^2$  for  $^{123}$ Sb (I=7/2) are used to calculate  $\nu_Q$ . The experimental  $\nu_Q$  and  $\eta$  are taken from Ref. [13] for skutterudites and from Ref. [14] for USb<sub>2</sub>.

material	a (Å)	u	v	Method used	$V_{zz} (10^{22} \text{ V/m}^2)$	$^{121}\nu_Q~(\mathrm{MHz})$		$^{123}\nu_Q~(\mathrm{MHz})$		$\eta$	
				in calculation	Calc.	Calc.	Exp.	Calc.	Exp.	Calc.	Exp.
$LaRu_4Sb_{12}$	9.27736	0.34208	0.15837	LDA	-1.9682	42.118	41.171	25.171	24.994	0.3816	0.406
$\mathrm{CeRu_4Sb_{12}}$	9.27215	0.34104	0.15773	LDA	-1.9953	42.698	41.358	25.846	25.108	0.3732	0.401
$PrRu_4Sb_{12}$	9.27013	0.34107	0.15723	$\mathrm{LDA}\!+\!U$	-1.9752	42.267	41.516	25.585	25.204	0.4341	0.402
$LaOs_4Sb_{12}$	9.30807	0.34140	0.15660	LDA	-2.0159	43.138	43.777	26.113	26.576	0.4503	0.450
$CeOs_4Sb_{12}$	9.30310	0.34043	0.15628	LDA	-2.0329	43.502	43.847	26.333	26.628	0.4523	0.463
$PrOs_4Sb_{12}$	9.30311	0.34050	0.15608	$\mathrm{LDA} + U$	-2.0415	43.686	44.167	26.444	26.810	0.5281	0.459
				4f as core	-2.0429	43.715		26.462		0.4401	
				$4f^0$	-2.0261	43.356		26.245		0.4386	
				LDA	-2.0345	43.535		26.353		0.4590	
USb <sub>2</sub> (S	$Sb_{I}$ )			LDA	-2.7971	59.855	60	36.232	37	0	0
(S	$b_{II})$			LDA	1.0211	21.851	19.4	13.227	11.8	0	0

as spherical core electrons ("4f as core" in Table 1), ii) Pr is replaced by La with the lattice parameters kept (" $4f^0$ " in Table 1), iii) 4f electrons are treated as itinerant electrons by using LDA. Remember that the Fermi surfaces of  $PrOs_4Sb_{12}$  are well reproduced by the LDA+U calculation [11].

For LaRu<sub>4</sub>Sb<sub>12</sub> and LaOs<sub>4</sub>Sb<sub>12</sub>, the calculated EFG reproduce well the experimental  $\nu_Q$  and asymmetry parameter  $\eta$ . Here parameters such as Q are used for  $\nu_Q$ , but no adjustable parameters are used for  $\eta$ . When the lattice constant is reduced, EFG increases in general. In fact,  $\nu_Q$  for Pr is larger than for La. Such a tendency is qualitatively reproduced in calculations. But, the difference of  $\nu_Q$  is too small to be discussed.

The LDA+U calculations for  $PrRu_4Sb_{12}$  and  $PrOs_4Sb_{12}$  show that  $\nu_Q$  are almost unchanged, but  $\eta$ increase, due to the anisotropic charge distribution on Pr-site. This is because  $V_{bc}$  is increased for the LDA+Ucalculation in both Pr compounds. It should be noted that  $V_{bc}$  is directed to the Pr position from (0, u, v). However, the measured  $\eta$  seem to be independent on La, Ce and Pr. Moreover, the recent careful experiment shows that  $\eta$  decreases with decreasing temperatures in  $PrOs_4Sb_{12}$  [15]. The discrepancy of  $\eta$  in both Pr skutterudites implies that the internal parameters of Sb site, which are experimentally obtained in room temperatures, are changed in low temperatures, affected by the anisotropic  $4f^2$  electrons. It means that Sb moves its position and the cage changes its shape in low temperatures. To confirm it, the calculations with other Sb positions are necessary.

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